# 14. Quadratic Equations

# Exercise 14.1

## 1. Question

Solve the following quadratic equations by factorization method

 $x^2 + 1 = 0$ 

## Answer

Given  $x^2 + 1 = 0$ We have  $i^2 = -1 \Rightarrow 1 = -i^2$ By substituting  $1 = -i^2$  in the above equation, we get  $x^2 - i^2 = 0$   $\Rightarrow (x + i)(x - i) = 0 [\because a^2 - b^2 = (a + b)(a - b)]$   $\Rightarrow x + i = 0 \text{ or } x - i = 0$   $\Rightarrow x = -i \text{ or } x = i$  $\therefore x = \pm i$ 

Thus, the roots of the given equation are  $\pm i$ .

## 2. Question

Solve the following quadratic equations by factorization method

 $9x^2 + 4 = 0$ 

## Answer

Given  $9x^2 + 4 = 0$   $\Rightarrow 9x^2 + 4 \times 1 = 0$ We have  $i^2 = -1 \Rightarrow 1 = -i^2$ By substituting  $1 = -i^2$  in the above equation, we get  $9x^2 + 4(-i^2) = 0$   $\Rightarrow 9x^2 - 4i^2 = 0$   $\Rightarrow (3x)^2 - (2i)^2 = 0$   $\Rightarrow (3x + 2i)(3x - 2i) = 0 [\because a^2 - b^2 = (a + b)(a - b)]$   $\Rightarrow 3x + 2i = 0 \text{ or } 3x - 2i = 0$   $\Rightarrow 3x = -2i \text{ or } 3x = 2i$   $\Rightarrow x = -\frac{2}{3}i \text{ or } \frac{2}{3}i$  $\Rightarrow x = \frac{2}{3}i \text{ or } \frac{2}{3}i$ 

Thus, the roots of the given equation are  $\pm \frac{2}{3}$  i.

## 3. Question

Solve the following quadratic equations by factorization method

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 $x^2 + 2x + 5 = 0$ 

#### Answer

Given  $x^2 + 2x + 5 = 0$   $\Rightarrow x^2 + 2x + 1 + 4 = 0$   $\Rightarrow x^2 + 2(x)(1) + 1^2 + 4 = 0$   $\Rightarrow (x + 1)^2 + 4 = 0 [\because (a + b)^2 = a^2 + 2ab + b^2]$   $\Rightarrow (x + 1)^2 + 4 \times 1 = 0$ We have  $i^2 = -1 \Rightarrow 1 = -i^2$ By substituting  $1 = -i^2$  in the above equation, we get  $(x + 1)^2 + 4(-i^2) = 0$   $\Rightarrow (x + 1)^2 - 4i^2 = 0$   $\Rightarrow (x + 1)^2 - (2i)^2 = 0$   $\Rightarrow (x + 1 + 2i)(x + 1 - 2i) = 0 [\because a^2 - b^2 = (a + b)(a - b)]$   $\Rightarrow x + 1 + 2i = 0 \text{ or } x + 1 - 2i = 0$  $\Rightarrow x = -1 - 2i \text{ or } x = -1 + 2i$ 

Thus, the roots of the given equation are  $-1 \pm 2i$ .

## 4. Question

Solve the following quadratic equations by factorization method

 $4x^2 - 12x + 25 = 0$ 

#### Answer

Given  $4x^2 - 12x + 25 = 0$   $\Rightarrow 4x^2 - 12x + 9 + 16 = 0$   $\Rightarrow (2x)^2 - 2(2x)(3) + 3^2 + 16 = 0$   $\Rightarrow (2x - 3)^2 + 16 = 0 [\because (a + b)^2 = a^2 + 2ab + b^2]$   $\Rightarrow (2x - 3)^2 + 16 \times 1 = 0$ We have  $i^2 = -1 \Rightarrow 1 = -i^2$ By substituting  $1 = -i^2$  in the above equation, we get  $(2x - 3)^2 + 16(-i^2) = 0$   $\Rightarrow (2x - 3)^2 - 16i^2 = 0$   $\Rightarrow (2x - 3)^2 - 16i^2 = 0$ Since  $a^2 - b^2 = (a + b)(a - b)$ , we get (2x - 3 + 4i)(2x - 3 - 4i) = 0  $\Rightarrow 2x - 3 + 4i = 0$  or 2x - 3 - 4i = 0 $\Rightarrow 2x = 3 - 4i$  or 2x = 3 + 4i

$$\Rightarrow x = \frac{3-4i}{2} \text{ or } \frac{3+4i}{2}$$
$$\Rightarrow x = \frac{3}{2} - 2i \text{ or } \frac{3}{2} + 2i$$
$$\therefore x = \frac{3}{2} \pm 2i$$

Thus, the roots of the given equation are  $\frac{3}{2} \pm 2i$ .

## 5. Question

Solve the following quadratic equations by factorization method

$$x^2 + x + 1 = 0$$

#### Answer

Given  $x^2 + x + 1 = 0$ 

$$\Rightarrow x^{2} + x + \frac{1}{4} + \frac{3}{4} = 0$$
  
$$\Rightarrow x^{2} + 2(x)\left(\frac{1}{2}\right) + \left(\frac{1}{2}\right)^{2} + \frac{3}{4} = 0$$
  
$$\Rightarrow \left(x + \frac{1}{2}\right)^{2} + \frac{3}{4} = 0 \ [\because (a + b)^{2} = a^{2} + 2ab + b^{2}]$$
  
$$\Rightarrow \left(x + \frac{1}{2}\right)^{2} + \frac{3}{4} \times 1 = 0$$

We have  $i^2 = -1 \Rightarrow 1 = -i^2$ 

By substituting  $1 = -i^2$  in the above equation, we get

$$\left(x + \frac{1}{2}\right)^2 + \frac{3}{4}(-i^2) = 0$$

$$\Rightarrow \left(x + \frac{1}{2}\right)^2 - \frac{3}{4}i^2 = 0$$

$$\Rightarrow \left(x + \frac{1}{2}\right)^2 - \left(\frac{\sqrt{3}}{2}i\right)^2 = 0$$

$$\Rightarrow \left(x + \frac{1}{2} + \frac{\sqrt{3}}{2}i\right) \left(x + \frac{1}{2} - \frac{\sqrt{3}}{2}i\right) = 0 [\because a^2 - b^2 = (a + b)(a - b)]$$

$$\Rightarrow x + \frac{1}{2} + \frac{\sqrt{3}}{2}i = 0 \text{ or } x + \frac{1}{2} - \frac{\sqrt{3}}{2}i = 0$$

$$\Rightarrow x = -\frac{1}{2} - \frac{\sqrt{3}}{2}i = 0 \text{ or } x = -\frac{1}{2} + \frac{\sqrt{3}}{2}i$$

$$\therefore x = -\frac{1}{2} \pm \frac{\sqrt{3}}{2}i$$

Thus, the roots of the given equation are  $-\frac{1}{2} \pm \frac{\sqrt{3}}{2}i$ .

## 6. Question

Solve the following quadratics

 $4x^{2} + 1 = 0$ **Answer** 





Given  $4x^2 + 1 = 0$ We have  $i^2 = -1 \Rightarrow 1 = -i^2$ By substituting  $1 = -i^2$  in the above equation, we get  $4x^2 - i^2 = 0$   $\Rightarrow (2x)^2 - i^2 = 0$   $\Rightarrow (2x + i)(2x - i) = 0 [\because a^2 - b^2 = (a + b)(a - b)]$   $\Rightarrow 2x + i = 0 \text{ or } 2x - i = 0$   $\Rightarrow 2x = -i \text{ or } 2x = i$   $\Rightarrow x = -\frac{1}{2}i \text{ or } \frac{1}{2}i$  $\therefore x = \pm \frac{1}{2}i$ 

Thus, the roots of the given equation are  $\pm \frac{1}{2}i$ .

## 7. Question

Solve the following quadratics

 $x^2 - 4x + 7 = 0$ 

## Answer

Given  $x^2 - 4x + 7 = 0$  $\Rightarrow x^2 - 4x + 4 + 3 = 0$  $\Rightarrow x^2 - 2(x)(2) + 2^2 + 3 = 0$  $\Rightarrow (x - 2)^{2} + 3 = 0$  [: (a - b)<sup>2</sup> = a<sup>2</sup> - 2ab + b<sup>2</sup>]  $\Rightarrow (x - 2)^2 + 3 \times 1 = 0$ We have  $i^2 = -1 \Rightarrow 1 = -i^2$ By substituting  $1 = -i^2$  in the above equation, we get  $(x - 2)^2 + 3(-i^2) = 0$  $\Rightarrow (x - 2)^2 - 3i^2 = 0$  $\Rightarrow (x-2)^2 - \left(\sqrt{3}i\right)^2 = 0$ Since  $a^2 - b^2 = (a + b)(a - b)$ , we get  $(x-2+\sqrt{3}i)(x-2-\sqrt{3}i)=0$  $\Rightarrow$  x - 2 +  $\sqrt{3}i = 0$  or x - 2 -  $\sqrt{3}i = 0$  $\Rightarrow$  x = 2 -  $\sqrt{3}i$  or x = 2 +  $\sqrt{3}i$  $\therefore x = 2 \pm \sqrt{3}i$ Thus, the roots of the given equation are  $2 \pm \sqrt{3}i$ .

## 8. Question

Solve the following quadratics



 $x^2 + 2x + 2 = 0$ 

#### Answer

Given  $x^2 + 2x + 2 = 0$   $\Rightarrow x^2 + 2x + 1 + 1 = 0$   $\Rightarrow x^2 + 2(x)(1) + 1^2 + 1 = 0$   $\Rightarrow (x + 1)^2 + 1 = 0 [\because (a + b)^2 = a^2 + 2ab + b^2]$ We have  $i^2 = -1 \Rightarrow 1 = -i^2$ By substituting  $1 = -i^2$  in the above equation, we get  $(x + 1)^2 + (-i^2) = 0$   $\Rightarrow (x + 1)^2 - i^2 = 0$   $\Rightarrow (x + 1)^2 - (i)^2 = 0$   $\Rightarrow (x + 1 + i)(x + 1 - i) = 0 [\because a^2 - b^2 = (a + b)(a - b)]$   $\Rightarrow x + 1 + i = 0 \text{ or } x + 1 - i = 0$   $\Rightarrow x = -1 - i \text{ or } x = -1 + i$  $\therefore x = -1 \pm i$ 

Thus, the roots of the given equation are  $-1 \pm i$ .

## 9. Question

Solve the following quadratics

 $5x^2 - 6x + 2 = 0$ 

#### Answer

Given  $5x^2 - 6x + 2 = 0$ 

Recall that the roots of quadratic equation  $ax^2 + bx + c = 0$ , where  $a \neq 0$ , are given by

$$\mathbf{x} = \frac{-\mathbf{b} \pm \sqrt{\mathbf{b}^2 - 4\mathbf{a}\mathbf{c}}}{2\mathbf{a}}$$

Here, a = 5, b = -6 and c = 2

$$\Rightarrow x = \frac{-(-6) \pm \sqrt{(-6)^2 - 4(5)(2)}}{2(5)}$$
$$\Rightarrow x = \frac{6 \pm \sqrt{36 - 40}}{10}$$
$$\Rightarrow x = \frac{6 \pm \sqrt{-4}}{10}$$
$$\Rightarrow x = \frac{6 \pm \sqrt{-4}}{10}$$
We have i<sup>2</sup> = -1

By substituting  $-1 = i^2$  in the above equation, we get

$$x = \frac{6 \pm \sqrt{4i^2}}{10}$$



$$\Rightarrow x = \frac{6 \pm \sqrt{(2i)^2}}{10}$$
$$\Rightarrow x = \frac{6 \pm 2i}{10}$$
$$\Rightarrow x = \frac{2(3 \pm i)}{10}$$
$$\Rightarrow x = \frac{3 \pm i}{5}$$
$$\therefore x = \frac{3}{5} \pm \frac{1}{5}i$$

Thus, the roots of the given equation are  $\frac{3}{5} \pm \frac{1}{5}i$ .

#### 10. Question

Solve the following quadratics

 $21x^2 + 9x + 1 = 0$ 

#### Answer

Given  $21x^2 + 9x + 1 = 0$ 

Recall that the roots of quadratic equation  $ax^2 + bx + c = 0$ , where  $a \neq 0$ , are given by

$$\mathbf{x} = \frac{-\mathbf{b} \pm \sqrt{\mathbf{b}^2 - 4\mathbf{ac}}}{2\mathbf{a}}$$
Here, a = 21, b = 9 and c =  

$$\Rightarrow \mathbf{x} = \frac{-9 \pm \sqrt{9^2 - 4(21)(1)}}{2(21)}$$

$$\Rightarrow \mathbf{x} = \frac{-9 \pm \sqrt{81 - 84}}{42}$$

$$\Rightarrow \mathbf{x} = \frac{-9 \pm \sqrt{-3}}{42}$$

$$\Rightarrow \mathbf{x} = \frac{-9 \pm \sqrt{-3}}{42}$$

We have  $i^2 = -1$ 

By substituting  $-1 = i^2$  in the above equation, we get

= 1

 $x = \frac{-9 \pm \sqrt{3i^2}}{42}$  $\Rightarrow x = \frac{-9 \pm \sqrt{\left(\sqrt{3}i\right)^2}}{42}$  $\Rightarrow x = \frac{-9 \pm \sqrt{3}i}{42}$  $\Rightarrow x = -\frac{9}{42} \pm \frac{\sqrt{3}}{42}i$  $\therefore x = -\frac{3}{14} \pm \frac{\sqrt{3}}{42}i$ 





Thus, the roots of the given equation are  $-\frac{3}{14} \pm \frac{\sqrt{3}}{42}i$ .

## 11. Question

Solve the following quadratics

$$x^2 - x + 1 = 0$$

## Answer

Given  $x^2 - x + 1 = 0$   $\Rightarrow x^2 - x + \frac{1}{4} + \frac{3}{4} = 0$   $\Rightarrow x^2 - 2(x)(\frac{1}{2}) + (\frac{1}{2})^2 + \frac{3}{4} = 0$   $\Rightarrow (x - \frac{1}{2})^2 + \frac{3}{4} = 0 [\because (a - b)^2 = a^2 - 2ab + b^2]$  $\Rightarrow (x - \frac{1}{2})^2 + \frac{3}{4} \times 1 = 0$ 

We have  $i^2 = -1 \Rightarrow 1 = -i^2$ 

By substituting  $1 = -i^2$  in the above equation, we get

$$\left(x - \frac{1}{2}\right)^{2} + \frac{3}{4}(-i^{2}) = 0$$
  

$$\Rightarrow \left(x - \frac{1}{2}\right)^{2} - \frac{3}{4}i^{2} = 0$$
  

$$\Rightarrow \left(x - \frac{1}{2}\right)^{2} - \left(\frac{\sqrt{3}}{2}i\right)^{2} = 0$$
  

$$\Rightarrow \left(x - \frac{1}{2} + \frac{\sqrt{3}}{2}i\right) \left(x - \frac{1}{2} - \frac{\sqrt{3}}{2}i\right) = 0 [\because a^{2} - b^{2} = (a + b)(a - b)]$$
  

$$\Rightarrow x - \frac{1}{2} + \frac{\sqrt{3}}{2}i = 0 \text{ or } x - \frac{1}{2} - \frac{\sqrt{3}}{2}i = 0$$
  

$$\Rightarrow x = \frac{1}{2} - \frac{\sqrt{3}}{2}i = 0 \text{ or } x = \frac{1}{2} + \frac{\sqrt{3}}{2}i$$
  

$$\therefore x = \frac{1}{2} \pm \frac{\sqrt{3}}{2}i$$

Thus, the roots of the given equation are  $\frac{1}{2} \pm \frac{\sqrt{3}}{2}i$ .

## 12. Question

Solve the following quadratics

 $x^2 + x + 1 = 0$ 

## Answer

Given 
$$x^2 + x + 1 = 0$$
  
 $\Rightarrow x^2 + x + \frac{1}{4} + \frac{3}{4} = 0$   
 $\Rightarrow x^2 + 2(x)(\frac{1}{2}) + (\frac{1}{2})^2 + \frac{3}{4} = 0$ 



$$\Rightarrow \left(x + \frac{1}{2}\right)^{2} + \frac{3}{4} = 0 \ [\because (a + b)^{2} = a^{2} + 2ab + b^{2}]$$
$$\Rightarrow \left(x + \frac{1}{2}\right)^{2} + \frac{3}{4} \times 1 = 0$$

We have  $i^2 = -1 \Rightarrow 1 = -i^2$ 

By substituting  $1 = -i^2$  in the above equation, we get

$$\left(x + \frac{1}{2}\right)^2 + \frac{3}{4}(-i^2) = 0$$

$$\Rightarrow \left(x + \frac{1}{2}\right)^2 - \frac{3}{4}i^2 = 0$$

$$\Rightarrow \left(x + \frac{1}{2}\right)^2 - \left(\frac{\sqrt{3}}{2}i\right)^2 = 0$$

$$\Rightarrow \left(x + \frac{1}{2} + \frac{\sqrt{3}}{2}i\right) \left(x + \frac{1}{2} - \frac{\sqrt{3}}{2}i\right) = 0 [\because a^2 - b^2 = (a + b)(a - b)]$$

$$\Rightarrow x + \frac{1}{2} + \frac{\sqrt{3}}{2}i = 0 \text{ or } x + \frac{1}{2} - \frac{\sqrt{3}}{2}i = 0$$

$$\Rightarrow x = -\frac{1}{2} - \frac{\sqrt{3}}{2}i = 0 \text{ or } x = -\frac{1}{2} + \frac{\sqrt{3}}{2}i$$

$$\therefore x = -\frac{1}{2} \pm \frac{\sqrt{3}}{2}i$$

Thus, the roots of the given equation are  $-\frac{1}{2} \pm \frac{\sqrt{3}}{2}$ i.

#### 13. Question

Solve the following quadratics

 $17x^2 - 8x + 1 = 0$ 

### Answer

Given  $17x^2 - 8x + 1 = 0$ 

Recall that the roots of quadratic equation  $ax^2 + bx + c = 0$ , where  $a \neq 0$ , are given by

$$\mathbf{x} = \frac{-\mathbf{b} \pm \sqrt{\mathbf{b}^2 - 4\mathbf{a}\mathbf{c}}}{2\mathbf{a}}$$

Here, a = 17, b = -8 and c = 1

$$\Rightarrow x = \frac{-(-8) \pm \sqrt{(-8)^2 - 4(17)(1)}}{2(17)}$$
$$\Rightarrow x = \frac{8 \pm \sqrt{64 - 68}}{34}$$
$$\Rightarrow x = \frac{8 \pm \sqrt{-4}}{34}$$
$$\Rightarrow x = \frac{8 \pm \sqrt{-4}}{34}$$
We have i<sup>2</sup> = -1

By substituting  $-1 = i^2$  in the above equation, we get





$$x = \frac{8 \pm \sqrt{4i^2}}{34}$$
  

$$\Rightarrow x = \frac{8 \pm \sqrt{(2i)^2}}{34}$$
  

$$\Rightarrow x = \frac{8 \pm 2i}{34}$$
  

$$\Rightarrow x = \frac{2(4 \pm i)}{34}$$
  

$$\Rightarrow x = \frac{4 \pm i}{17}$$
  

$$\therefore x = \frac{4}{17} \pm \frac{1}{17}i$$

Thus, the roots of the given equation are  $\frac{4}{17} \pm \frac{1}{17}i$ .

## 14. Question

Solve the following quadratics

 $27x^2 - 10x + 1 = 0$ 

#### Answer

Given  $27x^2 - 10x + 1 = 0$ 

Recall that the roots of quadratic equation  $ax^2 + bx + c = 0$ , where  $a \neq 0$ , are given by

$$\mathbf{x} = \frac{-\mathbf{b} \pm \sqrt{\mathbf{b}^2 - 4\mathbf{ac}}}{2\mathbf{a}}$$
  
Here, a = 27, b = -10 and c = 1  
$$\Rightarrow \mathbf{x} = \frac{-(-10) \pm \sqrt{(-10)^2 - 4(27)(1)}}{2(27)}$$
$$\Rightarrow \mathbf{x} = \frac{10 \pm \sqrt{100 - 108}}{54}$$
$$\Rightarrow \mathbf{x} = \frac{10 \pm \sqrt{-8}}{54}$$
$$\Rightarrow \mathbf{x} = \frac{10 \pm \sqrt{-8}}{54}$$
  
We have i<sup>2</sup> = -1

By substituting  $-1 = i^2$  in the above equation, we get

$$x = \frac{10 \pm \sqrt{8i^2}}{54}$$
$$\Rightarrow x = \frac{10 \pm \sqrt{(2\sqrt{2}i)^2}}{54}$$
$$\Rightarrow x = \frac{10 \pm 2\sqrt{2}i}{54}$$
$$\Rightarrow x = \frac{10 \pm 2\sqrt{2}i}{54}$$
$$\Rightarrow x = \frac{2(5 \pm \sqrt{2}i)}{54}$$





$$\Rightarrow x = \frac{5 \pm \sqrt{2}i}{27}$$
$$\therefore x = \frac{5}{27} \pm \frac{\sqrt{2}}{27}i$$

Thus, the roots of the given equation are  $\frac{5}{27} \pm \frac{\sqrt{2}}{27}$ i.

#### 15. Question

Solve the following quadratics

 $17x^2 + 28x + 12 = 0$ 

#### Answer

Given  $17x^2 + 28x + 12 = 0$ 

Recall that the roots of quadratic equation  $ax^2 + bx + c = 0$ , where  $a \neq 0$ , are given by

$$\mathbf{x} = \frac{-\mathbf{b} \pm \sqrt{\mathbf{b}^2 - 4\mathbf{ac}}}{2\mathbf{a}}$$
  
Here, a = 17, b = 28 and c = 12

$$\Rightarrow x = \frac{-28 \pm \sqrt{28^2 - 4(17)(12)}}{2(17)}$$
$$\Rightarrow x = \frac{-28 \pm \sqrt{784 - 816}}{34}$$
$$\Rightarrow x = \frac{-28 \pm \sqrt{-32}}{34}$$
$$\Rightarrow x = \frac{-28 \pm \sqrt{-32}}{34}$$
$$\Rightarrow x = \frac{-28 \pm \sqrt{32(-1)}}{34}$$

We have  $i^2 = -1$ 

By substituting  $-1 = i^2$  in the above equation, we get

$$x = \frac{-28 \pm \sqrt{32i^2}}{34}$$

$$\Rightarrow x = \frac{-28 \pm \sqrt{(4\sqrt{2}i)^2}}{34}$$

$$\Rightarrow x = \frac{-28 \pm 4\sqrt{2}i}{34}$$

$$\Rightarrow x = \frac{2(-14 \pm 2\sqrt{2}i)}{34}$$

$$\Rightarrow x = \frac{2(-14 \pm 2\sqrt{2}i)}{34}$$

$$\Rightarrow x = -\frac{14 \pm 2\sqrt{2}i}{17}$$

$$\therefore x = -\frac{14}{17} \pm \frac{2\sqrt{2}}{17}i$$

Thus, the roots of the given equation are  $-\frac{14}{17} \pm \frac{2\sqrt{2}}{17}i$ .

## 16. Question

Solve the following quadratics





 $21x^2 - 28x + 10 = 0$ 

#### Answer

Given  $21x^2 - 28x + 10 = 0$ 

Recall that the roots of quadratic equation  $ax^2 + bx + c = 0$ , where  $a \neq 0$ , are given by

$$\mathbf{x} = \frac{-\mathbf{b} \pm \sqrt{\mathbf{b}^2 - 4\mathbf{a}\mathbf{c}}}{2\mathbf{a}}$$

Here, a = 21, b = -28 and c = 10

$$\Rightarrow x = \frac{-(-28) \pm \sqrt{(-28)^2 - 4(21)(10)}}{2(21)}$$
$$\Rightarrow x = \frac{28 \pm \sqrt{784 - 840}}{42}$$
$$\Rightarrow x = \frac{28 \pm \sqrt{-56}}{42}$$
$$\Rightarrow x = \frac{28 \pm \sqrt{-56}}{42}$$
We have i<sup>2</sup> = -1

By substituting  $-1 = i^2$  in the above equation, we get

$$x = \frac{28 \pm \sqrt{56i^2}}{42}$$

$$\Rightarrow x = \frac{28 \pm \sqrt{(2\sqrt{14}i)^2}}{42}$$

$$\Rightarrow x = \frac{28 \pm 2\sqrt{14}i}{42}$$

$$\Rightarrow x = \frac{2(14 \pm \sqrt{14}i)}{42}$$

$$\Rightarrow x = \frac{14 \pm \sqrt{14}i}{21}$$

$$\Rightarrow x = \frac{14 \pm \sqrt{14}i}{21}$$

$$\Rightarrow x = \frac{14}{21} \pm \frac{\sqrt{14}}{21}i$$

$$\therefore x = \frac{2}{3} \pm \frac{\sqrt{14}}{21}i$$

Thus, the roots of the given equation are  $\frac{2}{3} \pm \frac{\sqrt{14}}{21}$ i.

## 17. Question

Solve the following quadratics

 $8x^2 - 9x + 3 = 0$ 

#### Answer

Given  $8x^2 - 9x + 3 = 0$ 

Recall that the roots of quadratic equation  $ax^2 + bx + c = 0$ , where  $a \neq 0$ , are given by

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$$\mathbf{x} = \frac{-\mathbf{b} \pm \sqrt{\mathbf{b}^2 - 4\mathbf{ac}}}{2\mathbf{a}}$$

Here, a = 8, b = -9 and c = 1

$$\Rightarrow x = \frac{-(-9) \pm \sqrt{(-9)^2 - 4(8)(3)}}{2(8)}$$
$$\Rightarrow x = \frac{9 \pm \sqrt{81 - 96}}{16}$$
$$\Rightarrow x = \frac{9 \pm \sqrt{-15}}{16}$$
$$\Rightarrow x = \frac{9 \pm \sqrt{-15}}{16}$$

We have  $i^2 = -1$ 

By substituting  $-1 = i^2$  in the above equation, we get

$$x = \frac{9 \pm \sqrt{15i^2}}{16}$$
$$\Rightarrow x = \frac{9 \pm \sqrt{(\sqrt{15i})^2}}{16}$$
$$\Rightarrow x = \frac{9 \pm \sqrt{15i}}{16}$$
$$\therefore x = \frac{9 \pm \sqrt{15i}}{16} \pm \frac{\sqrt{15}}{16}i$$

Thus, the roots of the given equation are  $\frac{9}{16} \pm \frac{\sqrt{15}}{16}i$ .

## 18. Question

Solve the following quadratics

 $13x^2 + 7x + 1 = 0$ 

#### Answer

Given  $13x^2 + 7x + 1 = 0$ 

Recall that the roots of quadratic equation  $ax^2 + bx + c = 0$ , where  $a \neq 0$ , are given by

$$\mathbf{x} = \frac{-\mathbf{b} \pm \sqrt{\mathbf{b}^2 - 4\mathbf{a}\mathbf{c}}}{2\mathbf{a}}$$

Here, a = 13, b = 7 and c = 1

$$\Rightarrow x = \frac{-7 \pm \sqrt{7^2 - 4(13)(1)}}{2(13)}$$
$$\Rightarrow x = \frac{-7 \pm \sqrt{49 - 52}}{26}$$
$$\Rightarrow x = \frac{-7 \pm \sqrt{-3}}{26}$$
$$\Rightarrow x = \frac{-7 \pm \sqrt{-3}}{26}$$
$$\Rightarrow x = \frac{-7 \pm \sqrt{3(-1)}}{26}$$



By substituting  $-1 = i^2$  in the above equation, we get

$$x = \frac{-7 \pm \sqrt{3i^2}}{26}$$
$$\Rightarrow x = \frac{-7 \pm \sqrt{(\sqrt{3}i)^2}}{26}$$
$$\Rightarrow x = \frac{-7 \pm \sqrt{3i}}{26}$$
$$\therefore x = -\frac{7}{26} \pm \frac{\sqrt{3}}{26}i$$

Thus, the roots of the given equation are  $-\frac{7}{26} \pm \frac{\sqrt{3}}{26}$ i.

#### **19.** Question

 $2x^2 + x + 1 = 0$ 

#### Answer

Given  $2x^2 + x + 1 = 0$ 

Recall that the roots of quadratic equation  $ax^2 + bx + c = 0$ , where  $a \neq 0$ , are given by

$$\mathbf{x} = \frac{-\mathbf{b} \pm \sqrt{\mathbf{b}^2 - 4\mathbf{a}\mathbf{c}}}{2\mathbf{a}}$$

Here, a = 2, b = 1 and c = 1

$$\Rightarrow x = \frac{-1 \pm \sqrt{1^2 - 4(2)(1)}}{2(2)}$$
$$\Rightarrow x = \frac{-1 \pm \sqrt{1 - 8}}{4}$$
$$\Rightarrow x = \frac{-1 \pm \sqrt{-7}}{4}$$
$$\Rightarrow x = \frac{-1 \pm \sqrt{-7}}{4}$$

We have  $i^2 = -1$ 

By substituting  $-1 = i^2$  in the above equation, we get

$$x = \frac{-1 \pm \sqrt{7i^2}}{4}$$
  
$$\Rightarrow x = \frac{-1 \pm \sqrt{(\sqrt{7}i)^2}}{4}$$
  
$$\Rightarrow x = \frac{-1 \pm \sqrt{7i}}{4}$$
  
$$\therefore x = -\frac{1}{4} \pm \frac{\sqrt{7}}{4}i$$

Thus, the roots of the given equation are  $-\frac{1}{4} \pm \frac{\sqrt{7}}{4}i$ .





#### 20. Question

Prove: 
$$\sqrt{3}x^2 - \sqrt{2}x + 3\sqrt{3} = 0$$

# Answer

Given  $\sqrt{3}x^2 - \sqrt{2}x + 3\sqrt{3} = 0$ 

Recall that the roots of quadratic equation  $ax^2 + bx + c = 0$ , where  $a \neq 0$ , are given by

$$\mathbf{x} = \frac{-\mathbf{b} \pm \sqrt{\mathbf{b}^2 - 4\mathbf{ac}}}{2\mathbf{a}}$$
Here,  $\mathbf{a} = \sqrt{3}$ ,  $\mathbf{b} = -\sqrt{2}$  and  $\mathbf{c} = 3\sqrt{3}$ 

$$\Rightarrow \mathbf{x} = \frac{-(-\sqrt{2}) \pm \sqrt{(-\sqrt{2})^2 - 4(\sqrt{3})(3\sqrt{3})}}{2(\sqrt{3})}$$

$$\Rightarrow \mathbf{x} = \frac{\sqrt{2} \pm \sqrt{2 - 36}}{2\sqrt{3}}$$

$$\Rightarrow \mathbf{x} = \frac{\sqrt{2} \pm \sqrt{-34}}{2\sqrt{3}}$$

$$\Rightarrow \mathbf{x} = \frac{-\sqrt{2} \pm \sqrt{-34}}{2\sqrt{3}}$$

$$\Rightarrow \mathbf{x} = \frac{-\sqrt{2} \pm \sqrt{34(-1)}}{2\sqrt{3}}$$

We have  $i^2 = -1$ 

By substituting  $-1 = i^2$  in the above equation, we get

$$x = \frac{-\sqrt{2} \pm \sqrt{34i^2}}{2\sqrt{3}}$$
$$\Rightarrow x = \frac{-\sqrt{2} \pm \sqrt{(\sqrt{34i})^2}}{2\sqrt{3}}$$
$$\Rightarrow x = \frac{-\sqrt{2} \pm \sqrt{34i}}{2\sqrt{3}}$$
$$\therefore x = -\frac{\sqrt{2} \pm \sqrt{34i}}{2\sqrt{3}} \pm \frac{\sqrt{34}}{2\sqrt{3}}i$$

Thus, the roots of the given equation are  $-\frac{\sqrt{2}}{2\sqrt{3}}\pm\frac{\sqrt{34}}{2\sqrt{3}}i\cdot$ 

### 21. Question

Solve the following quadratics  $\sqrt{2}x^2 + x + \sqrt{2} = 0$ 

#### Answer

Given  $\sqrt{2}x^2 + x + \sqrt{2} = 0$ 

Recall that the roots of quadratic equation  $ax^2 + bx + c = 0$ , where  $a \neq 0$ , are given by

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$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$
 Here,  $_a = \sqrt{2}, \, b = 1$  and  $_c = \sqrt{2}$ 

$$\Rightarrow x = \frac{-1 \pm \sqrt{1^2 - 4(\sqrt{2})(\sqrt{2})}}{2(\sqrt{2})}$$
$$\Rightarrow x = \frac{-1 \pm \sqrt{1 - 8}}{2\sqrt{2}}$$
$$\Rightarrow x = \frac{-1 \pm \sqrt{-7}}{2\sqrt{2}}$$
$$\Rightarrow x = \frac{-1 \pm \sqrt{7(-1)}}{2\sqrt{2}}$$

By substituting  $-1 = i^2$  in the above equation, we get

$$x = \frac{-1 \pm \sqrt{7i^2}}{2\sqrt{2}}$$
$$\Rightarrow x = \frac{-1 \pm \sqrt{(\sqrt{7}i)^2}}{2\sqrt{2}}$$
$$\Rightarrow x = \frac{-1 \pm \sqrt{7i}}{2\sqrt{2}}$$
$$\therefore x = -\frac{1 \pm \sqrt{7i}}{2\sqrt{2}} \pm \frac{\sqrt{7}}{2\sqrt{2}}i$$

Thus, the roots of the given equation are  $-\frac{1}{2\sqrt{2}} \pm \frac{\sqrt{7}}{2\sqrt{2}}i$ .

## 22. Question

Solve the following quadratics  $x^2 + x + \frac{1}{\sqrt{2}} = 0$ 

#### Answer

Given  $x^2 + x + \frac{1}{\sqrt{2}} = 0$  $\Rightarrow \left(x^2 + x + \frac{1}{\sqrt{2}}\right) \times \sqrt{2} = 0 \times \sqrt{2}$   $\Rightarrow \sqrt{2}x^2 + \sqrt{2}x + 1 = 0$ 

Recall that the roots of quadratic equation  $ax^2 + bx + c = 0$ , where  $a \neq 0$ , are given by

$$\mathbf{x} = \frac{-\mathbf{b} \pm \sqrt{\mathbf{b}^2 - 4\mathbf{a}\mathbf{c}}}{2\mathbf{a}}$$

Here,  $_{a}=\sqrt{2},$   $_{b}=\sqrt{2}$  and  $_{c}=1$ 

$$\Rightarrow x = \frac{-\sqrt{2} \pm \sqrt{(\sqrt{2})^2 - 4(\sqrt{2})(1)}}{2(\sqrt{2})}$$
$$\Rightarrow x = \frac{-\sqrt{2} \pm \sqrt{2 - 4\sqrt{2}}}{2\sqrt{2}}$$



$$\Rightarrow x = \frac{-\sqrt{2} \pm \sqrt{2(1 - 2\sqrt{2})}}{2\sqrt{2}}$$
$$\Rightarrow x = \frac{-\sqrt{2} \pm \sqrt{2} \times \sqrt{1 - 2\sqrt{2}}}{2\sqrt{2}}$$
$$\Rightarrow x = \frac{\sqrt{2}(-1 \pm \sqrt{1 - 2\sqrt{2}})}{2\sqrt{2}}$$
$$\Rightarrow x = \frac{-1 \pm \sqrt{1 - 2\sqrt{2}}}{2}$$
$$\Rightarrow x = \frac{-1 \pm \sqrt{1 - 2\sqrt{2}}}{2}$$

By substituting  $-1 = i^2$  in the above equation, we get

$$x = \frac{-1 \pm \sqrt{(2\sqrt{2} - 1)i^2}}{2}$$
$$\Rightarrow x = \frac{-1 \pm \sqrt{(\sqrt{2\sqrt{2} - 1}i)^2}}{2}$$
$$\Rightarrow x = \frac{-1 \pm \sqrt{2\sqrt{2} - 1}i}{2}$$
$$\therefore x = -\frac{1}{2} \pm \frac{\sqrt{2\sqrt{2} - 1}i}{2}i$$

Thus, the roots of the given equation are  $-\frac{1}{2} \pm \frac{\sqrt{2\sqrt{2}-1}}{2}i$ .

## 23. Question

Solve: 
$$x^2 + \frac{x}{\sqrt{2}} + 1 = 0$$

#### Answer

Given 
$$x^2 + \frac{x}{\sqrt{2}} + 1 = 0$$
  

$$\Rightarrow \left(x^2 + \frac{x}{\sqrt{2}} + 1\right) \times \sqrt{2} = 0 \times \sqrt{2}$$

$$\Rightarrow \sqrt{2}x^2 + x + \sqrt{2} = 0$$

Recall that the roots of quadratic equation  $ax^2 + bx + c = 0$ , where  $a \neq 0$ , are given by

$$\mathbf{x} = \frac{-\mathbf{b} \pm \sqrt{\mathbf{b}^2 - 4\mathbf{ac}}}{2\mathbf{a}}$$
  
Here,  $\mathbf{a} = \sqrt{2}$ ,  $\mathbf{b} = 1$  and  $\mathbf{c} = \sqrt{2}$ 
$$\Rightarrow \mathbf{x} = \frac{-1 \pm \sqrt{1^2 - 4(\sqrt{2})(\sqrt{2})}}{2(\sqrt{2})}$$



$$\Rightarrow x = \frac{-1 \pm \sqrt{1-8}}{2\sqrt{2}}$$
$$\Rightarrow x = \frac{-1 \pm \sqrt{-7}}{2\sqrt{2}}$$
$$\Rightarrow x = \frac{-1 \pm \sqrt{7}}{2\sqrt{2}}$$

By substituting  $-1 = i^2$  in the above equation, we get

$$x = \frac{-1 \pm \sqrt{7i^2}}{2\sqrt{2}}$$
$$\Rightarrow x = \frac{-1 \pm \sqrt{(\sqrt{7}i)^2}}{2\sqrt{2}}$$
$$\Rightarrow x = \frac{-1 \pm \sqrt{7i}}{2\sqrt{2}}$$
$$\therefore x = -\frac{1 \pm \sqrt{7i}}{2\sqrt{2}} \pm \frac{\sqrt{7}}{2\sqrt{2}}i$$

Thus, the roots of the given equation are  $-\frac{1}{2\sqrt{2}}\pm\frac{\sqrt{7}}{2\sqrt{2}}i$ .

#### 24. Question

Solve the following quadratics  $\sqrt{5}x^2+x+\sqrt{5}=0$ 

### Answer

Given  $\sqrt{5}x^2 + x + \sqrt{5} = 0$ 

Recall that the roots of quadratic equation  $ax^2 + bx + c = 0$ , where  $a \neq 0$ , are given by

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$$\mathbf{x} = \frac{-\mathbf{b} \pm \sqrt{\mathbf{b}^2 - 4\mathbf{a}\mathbf{c}}}{2\mathbf{a}}$$

Here,  $a = \sqrt{5}$ , b = 1 and  $c = \sqrt{5}$ 

$$\Rightarrow x = \frac{-1 \pm \sqrt{1^2 - 4(\sqrt{5})(\sqrt{5})}}{2(\sqrt{5})}$$
$$\Rightarrow x = \frac{-1 \pm \sqrt{1 - 20}}{2\sqrt{5}}$$
$$\Rightarrow x = \frac{-1 \pm \sqrt{-19}}{2\sqrt{5}}$$
$$\Rightarrow x = \frac{-1 \pm \sqrt{-19}}{2\sqrt{5}}$$
We have i<sup>2</sup> = -1

By substituting  $-1 = i^2$  in the above equation, we get

$$x = \frac{-1 \pm \sqrt{19i^2}}{2\sqrt{5}}$$
$$\Rightarrow x = \frac{-1 \pm \sqrt{(\sqrt{19i})^2}}{2\sqrt{5}}$$
$$\Rightarrow x = \frac{-1 \pm \sqrt{19i}}{2\sqrt{5}}$$
$$\therefore x = -\frac{1 \pm \sqrt{19i}}{2\sqrt{5}} \pm \frac{\sqrt{19i}}{2\sqrt{5}}$$

Thus, the roots of the given equation are  $-\frac{1}{2\sqrt{5}}\pm\frac{\sqrt{19}}{2\sqrt{5}}i$ .

### 25. Question

 $-x^2 + x - 2 = 0$ 

#### Answer

Given -x<sup>2</sup> + x - 2 = 0  
⇒ x<sup>2</sup> - x + 2 = 0  
⇒ x<sup>2</sup> - x + 
$$\frac{1}{4} + \frac{7}{4} = 0$$
  
⇒ x<sup>2</sup> - 2(x)( $\frac{1}{2}$ ) + ( $\frac{1}{2}$ )<sup>2</sup> +  $\frac{7}{4} = 0$   
⇒ (x -  $\frac{1}{2}$ )<sup>2</sup> +  $\frac{7}{4} = 0$  [∵ (a - b)<sup>2</sup> = a<sup>2</sup> - 2ab + b<sup>2</sup>]  
⇒ (x -  $\frac{1}{2}$ )<sup>2</sup> +  $\frac{7}{4} \times 1 = 0$ 

We have  $i^2 = -1 \Rightarrow 1 = -i^2$ 

By substituting  $1 = -i^2$  in the above equation, we get

$$\left(x - \frac{1}{2}\right)^2 + \frac{7}{4}(-i^2) = 0$$

$$\Rightarrow \left(x - \frac{1}{2}\right)^2 - \frac{7}{4}i^2 = 0$$

$$\Rightarrow \left(x - \frac{1}{2}\right)^2 - \left(\frac{\sqrt{7}}{2}i\right)^2 = 0$$

$$\Rightarrow \left(x - \frac{1}{2} + \frac{\sqrt{7}}{2}i\right) \left(x - \frac{1}{2} - \frac{\sqrt{7}}{2}i\right) = 0 \ [\because a^2 - b^2 = (a + b)(a - b)]$$

$$\Rightarrow x - \frac{1}{2} + \frac{\sqrt{7}}{2}i = 0 \ \text{or } x - \frac{1}{2} - \frac{\sqrt{7}}{2}i = 0$$

$$\Rightarrow x = \frac{1}{2} - \frac{\sqrt{7}}{2}i = 0 \ \text{or } x = \frac{1}{2} + \frac{\sqrt{7}}{2}i$$

$$\therefore x = \frac{1}{2} \pm \frac{\sqrt{7}}{2}i$$

Thus, the roots of the given equation are  $\frac{1}{2} \pm \frac{\sqrt{7}}{2}i$ .





#### 26. Question

Solve:  $x^2 - 2x + \frac{3}{2} = 0$ 

#### Answer

Given  $x^2 - 2x + \frac{3}{2} = 0$   $\Rightarrow x^2 - 2x + 1 + \frac{1}{2} = 0$   $\Rightarrow x^2 - 2(x)(\frac{1}{2}) + 1^2 + \frac{1}{2} = 0$   $\Rightarrow (x - 1)^2 + \frac{1}{2} = 0 [\because (a - b)^2 = a^2 - 2ab + b^2]$  $\Rightarrow (x - 1)^2 + \frac{1}{2} \times 1 = 0$ 

We have  $i^2 = -1 \Rightarrow 1 = -i^2$ 

By substituting  $1 = -i^2$  in the above equation, we get

$$(x-1)^{2} + \frac{1}{2}(-i^{2}) = 0$$
  

$$\Rightarrow (x-1)^{2} - \frac{1}{2}i^{2} = 0$$
  

$$\Rightarrow (x-1)^{2} - \left(\frac{1}{\sqrt{2}}i\right)^{2} = 0$$
  

$$\Rightarrow \left(x-1+\frac{1}{\sqrt{2}}i\right)\left(x-1-\frac{1}{\sqrt{2}}i\right) = 0 \ [\because a^{2} - b^{2} = (a+b)(a-b)]$$
  

$$\Rightarrow x-1+\frac{1}{\sqrt{2}}i = 0 \ \text{or} \ x - 1 - \frac{1}{\sqrt{2}}i = 0$$
  

$$\Rightarrow x = 1 - \frac{1}{\sqrt{2}}i = 0 \ \text{or} \ x = 1 + \frac{1}{\sqrt{2}}i$$
  

$$\therefore x = 1 \pm \frac{1}{\sqrt{2}}i$$

Thus, the roots of the given equation are  $1 \pm \frac{1}{\sqrt{2}}i$ .

## 27. Question

Solve the following quadratics  $3x^2 - 4x + \frac{20}{3} = 0$ 

#### Answer

Given  $3x^2 - 4x + \frac{20}{3} = 0$ 

Recall that the roots of quadratic equation  $ax^2 + bx + c = 0$ , where  $a \neq 0$ , are given by

$$\mathbf{x} = \frac{-\mathbf{b} \pm \sqrt{\mathbf{b}^2 - 4\mathbf{ac}}}{2\mathbf{a}}$$
  
Here, a = 3, b = -4 and c =  $\frac{20}{3}$ 

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$$\Rightarrow x = \frac{-(-4) \pm \sqrt{(-4)^2 - 4(3)\left(\frac{20}{3}\right)}}{2(3)}$$
$$\Rightarrow x = \frac{4 \pm \sqrt{16 - 80}}{6}$$
$$\Rightarrow x = \frac{4 \pm \sqrt{-64}}{6}$$
$$\Rightarrow x = \frac{4 \pm \sqrt{-64}}{6}$$

By substituting  $-1 = i^2$  in the above equation, we get

$$x = \frac{4 \pm \sqrt{64i^2}}{6}$$
  

$$\Rightarrow x = \frac{4 \pm \sqrt{(8i)^2}}{6}$$
  

$$\Rightarrow x = \frac{4 \pm 8i}{6}$$
  

$$\Rightarrow x = \frac{2(2 \pm 4i)}{6}$$
  

$$\Rightarrow x = \frac{2 \pm 4i}{3}$$
  

$$\therefore x = \frac{2}{3} \pm \frac{4}{3}i$$

Thus, the roots of the given equation are  $\frac{2}{3} \pm \frac{4}{3}i$ .

# Exercise 14.2

## **1 A. Question**

Solve the following quadratic equations by factorization method:

 $x^2 + 10ix - 21 = 0$ 

#### Answer

 $x^{2} + 10ix - 21 = 0$ Given  $x^{2} + 10ix - 21 = 0$   $\Rightarrow x^{2} + 10ix - 21 \times 1 = 0$ We have  $i^{2} = -1 \Rightarrow 1 = -i^{2}$ By substituting  $1 = -i^{2}$  in the above equation, we get  $x^{2} + 10ix - 21(-i^{2}) = 0$   $\Rightarrow x^{2} + 10ix + 21i^{2} = 0$   $\Rightarrow x^{2} + 3ix + 7ix + 21i^{2} = 0$   $\Rightarrow x(x + 3i) + 7i(x + 3i) = 0$  $\Rightarrow (x + 3i)(x + 7i) = 0$ 



 $\Rightarrow$  x + 3i = 0 or x + 7i = 0

∴ x = -3i or -7i

Thus, the roots of the given equation are -3i and -7i.

#### **1 B. Question**

Solve the following quadratic equations by factorization method:

 $x^{2} + (1 - 2i)x - 2i = 0$ 

#### Answer

 $x^{2} + (1 - 2i)x - 2i = 0$ Given x<sup>2</sup> + (1 - 2i)x - 2i = 0 ⇒ x<sup>2</sup> + x - 2ix - 2i = 0 ⇒ x(x + 1) - 2i(x + 1) = 0 ⇒ (x + 1)(x - 2i) = 0 ⇒ x + 1 = 0 or x - 2i = 0 ∴ x = -1 or 2i

Thus, the roots of the given equation are -1 and 2i.

### **1 C. Question**

Solve the following quadratic equations by factorization method:

$$x^2 - \left(2\sqrt{3} + 3i\right)x + 6\sqrt{3}i = 0$$

#### Answer

$$x^{2} - (2\sqrt{3} + 3i)x + 6\sqrt{3}i = 0$$
  
Given  $x^{2} - (2\sqrt{3} + 3i)x + 6\sqrt{3}i = 0$   
 $\Rightarrow x^{2} - (2\sqrt{3}x + 3ix) + 6\sqrt{3}i = 0$   
 $\Rightarrow x^{2} - 2\sqrt{3}x - 3ix + 6\sqrt{3}i = 0$   
 $\Rightarrow x(x - 2\sqrt{3}) - 3i(x - 2\sqrt{3}) = 0$   
 $\Rightarrow (x - 2\sqrt{3})(x - 3i) = 0$   
 $\Rightarrow x - 2\sqrt{3} = 0 \text{ or } x - 3i = 0$   
 $\therefore x = 2\sqrt{3} \text{ or } 3i$ 

Thus, the roots of the given equation are  $2\sqrt{3}$  and 3i.

## **1 D. Question**

Solve the following quadratic equations by factorization method:

 $6x^2 - 17ix - 12 = 0$ 

# Answer

 $6x^2 - 17ix - 12 = 0$ Given  $6x^2 - 17ix - 12 = 0$ 



 $\Rightarrow 6x^{2} - 17ix - 12 \times 1 = 0$ We have  $i^{2} = -1 \Rightarrow 1 = -i^{2}$ By substituting  $1 = -i^{2}$  in the above equation, we get  $6x^{2} - 17ix - 12(-i^{2}) = 0$  $\Rightarrow 6x^{2} - 17ix + 12i^{2} = 0$  $\Rightarrow 6x^{2} - 9ix - 8ix + 12i^{2} = 0$  $\Rightarrow 3x(2x - 3i) - 4i(2x - 3i) = 0$  $\Rightarrow (2x - 3i)(3x - 4i) = 0$  $\Rightarrow 2x - 3i = 0 \text{ or } 3x - 4i = 0$  $\Rightarrow 2x = 3i \text{ or } 3x = 4i$  $\therefore x = \frac{3}{2}i \text{ or } \frac{4}{3}i$ 

Thus, the roots of the given equation are  $\frac{3}{2}i$  and  $\frac{4}{3}i$ .

## 2 A. Question

Solve the following quadratic equations:

$$x^2 - \left(3\sqrt{2} + 2i\right)x + 6\sqrt{2}i = 0$$

### Answer

$$x^{2} - (3\sqrt{2} + 2i)x + 6\sqrt{2}i = 0$$
  
Given  $x^{2} - (3\sqrt{2} + 2i)x + 6\sqrt{2}i = 0$   
 $\Rightarrow x^{2} - (3\sqrt{2}x + 2ix) + 6\sqrt{2}i = 0$   
 $\Rightarrow x^{2} - 3\sqrt{2}x - 2ix + 6\sqrt{2}i = 0$   
 $\Rightarrow x(x - 3\sqrt{2}) - 2i(x - 3\sqrt{2}) = 0$   
 $\Rightarrow (x - 3\sqrt{2})(x - 2i) = 0$   
 $\Rightarrow x - 3\sqrt{2} = 0 \text{ or } x - 2i = 0$   
 $\therefore x = 3\sqrt{2} \text{ or } 2i$ 

Thus, the roots of the given equation are  $3\sqrt{2}$  and 2i.

## 2 B. Question

Solve the following quadratic equations:

 $x^{2} - (5 - i)x + (18 + i) = 0$ 

# Answer

$$x^{2} - (5 - i)x + (18 + i) = 0$$

Given  $x^2 - (5 - i)x + (18 + i) = 0$ 

Recall that the roots of quadratic equation  $ax^2 + bx + c = 0$ , where  $a \neq 0$ , are given by

$$\mathbf{x} = \frac{-\mathbf{b} \pm \sqrt{\mathbf{b}^2 - 4\mathbf{a}\mathbf{c}}}{2\mathbf{a}}$$





Here, a = 1, b = -(5 - i) and c = (18 + i)

$$\Rightarrow x = \frac{-(-(5-i)) \pm \sqrt{(-(5-i))^2 - 4(1)(18+i)}}{2(1)}$$
$$\Rightarrow x = \frac{(5-i) \pm \sqrt{(5-i)^2 - 4(18+i)}}{2}$$
$$\Rightarrow x = \frac{(5-i) \pm \sqrt{25 - 10i + i^2 - 72 - 4i}}{2}$$
$$\Rightarrow x = \frac{(5-i) \pm \sqrt{-47 - 14i + i^2}}{2}$$

By substituting  $i^2 = -1$  in the above equation, we get

$$x = \frac{(5-i) \pm \sqrt{-47 - 14i + (-1)}}{2}$$
  

$$\Rightarrow x = \frac{(5-i) \pm \sqrt{-48 - 14i}}{2}$$
  

$$\Rightarrow x = \frac{(5-i) \pm \sqrt{(-1)(48 + 14i)}}{2}$$

By substituting  $-1 = i^2$  in the above equation, we get

$$x = \frac{(5-i) \pm \sqrt{i^2(48+14i)}}{2}$$
  

$$\Rightarrow x = \frac{(5-i) \pm i\sqrt{48+14i}}{2}$$
  
We can write  $48 + 14i = 49 - 1 + 14i$   

$$\Rightarrow 48 + 14i = 49 + i^2 + 14i [\because i^2 = -1]$$
  

$$\Rightarrow 48 + 14i = 7^2 + i^2 + 2(7)(i)$$
  

$$\Rightarrow 48 + 14i = (7 + i)^2 [\because (a + b)^2 = a^2 + b^2 + 2ab]$$
  
By using the result  $48 + 14i = (7 + i)^2$ , we get

$$x = \frac{(5-i) \pm i\sqrt{(7+i)^2}}{2}$$
  

$$\Rightarrow x = \frac{(5-i) \pm i(7+i)}{2}$$
  

$$\Rightarrow x = \frac{(5-i) + i(7+i)}{2} \text{ or } \frac{(5-i) - i(7+i)}{2}$$
  

$$\Rightarrow x = \frac{5-i+7i+i^2}{2} \text{ or } \frac{5-i-7i-i^2}{2}$$
  

$$\Rightarrow x = \frac{5+6i+(-1)}{2} \text{ or } \frac{5-8i-(-1)}{2} [\because i^2 = -1]$$
  

$$\Rightarrow x = \frac{5+6i-1}{2} \text{ or } \frac{5-8i+1}{2}$$
  

$$\Rightarrow x = \frac{4+6i}{2} \text{ or } \frac{6-8i}{2}$$



$$\Rightarrow x = \frac{2(2+3i)}{2} \text{ or } \frac{2(3-4i)}{2}$$
$$\therefore x = 2 + 3i \text{ or } 3 - 4i$$

Thus, the roots of the given equation are 2 + 3i and 3 - 4i.

#### 2 C. Question

Solve the following quadratic equations:

 $(2 + i)x^2 - (5 - i)x + 2(1 - i) = 0$ 

#### Answer

 $(2 + i)x^2 - (5 - i)x + 2(1 - i) = 0$ 

Given  $(2 + i)x^2 - (5 - i)x + 2(1 - i) = 0$ 

Recall that the roots of quadratic equation  $ax^2 + bx + c = 0$ , where  $a \neq 0$ , are given by

$$\mathbf{x} = \frac{-\mathbf{b} \pm \sqrt{\mathbf{b}^2 - 4\mathbf{a}\mathbf{c}}}{2\mathbf{a}}$$

Here, a = (2 + i), b = -(5 - i) and c = 2(1 - i)

$$\Rightarrow x = \frac{-(-(5-i)) \pm \sqrt{(-(5-i))^2 - 4(2+i)(2(1-i))}}{2(2+i)}$$
$$\Rightarrow x = \frac{(5-i) \pm \sqrt{(5-i)^2 - 8(2+i)(1-i)}}{2(2+i)}$$
$$\Rightarrow x = \frac{(5-i) \pm \sqrt{25 - 10i + i^2 - 8(2-2i+i-i^2)}}{2(2+i)}$$

By substituting  $i^2 = -1$  in the above equation, we get

$$x = \frac{(5-i) \pm \sqrt{25 - 10i + (-1) - 8(2 - i - (-1))}}{2(2+i)}$$
  

$$\Rightarrow x = \frac{(5-i) \pm \sqrt{24 - 10i - 8(3-i)}}{2(2+i)}$$
  

$$\Rightarrow x = \frac{(5-i) \pm \sqrt{24 - 10i - 24 + 8i}}{2(2+i)}$$
  

$$\Rightarrow x = \frac{(5-i) \pm \sqrt{-2i}}{2(2+i)}$$
  
We can write  $-2i = -2i + 1 - 1$   

$$\Rightarrow -2i = -2i + 1 + i^{2} [\because i^{2} = -1]$$
  

$$\Rightarrow -2i = 1 - 2i + i^{2}$$
  

$$\Rightarrow -2i = 1^{2} - 2(1)(i) + i^{2}$$
  

$$\Rightarrow -2i = (1 - i)^{2} [\because (a - b)^{2} = a^{2} - 2ab + b^{2}]$$
  
By using the result  $-2i = (1 - i)^{2}$ , we get  

$$= (5-i) \pm \sqrt{(1-i)^{2}}$$

$$x = \frac{(3-i) \pm \sqrt{(1-i)}}{2(2+i)}$$



$$\Rightarrow x = \frac{(5-i) \pm (1-i)}{2(2+i)}$$
  

$$\Rightarrow x = \frac{(5-i) + (1-i)}{2(2+i)} \text{ or } \frac{(5-i) - (1-i)}{2(2+i)}$$
  

$$\Rightarrow x = \frac{5-i+1-i}{2(2+i)} \text{ or } \frac{5-i-1+i}{2(2+i)}$$
  

$$\Rightarrow x = \frac{5-i+1-i}{2(2+i)} \text{ or } \frac{4}{2(2+i)}$$
  

$$\Rightarrow x = \frac{6-2i}{2(2+i)} \text{ or } \frac{4}{2(2+i)}$$
  

$$\Rightarrow x = \frac{3-i}{2+i} \propto \frac{2-i}{2+i} \text{ or } \frac{2}{2+i}$$
  

$$\Rightarrow x = \frac{3-i}{2+i} \times \frac{2-i}{2-i} \text{ or } \frac{2}{2+i} \times \frac{2-i}{2-i}$$
  

$$\Rightarrow x = \frac{(3-i)(2-i)}{(2+i)(2-i)} \text{ or } \frac{2(2-i)}{(2+i)(2-i)}$$
  

$$\Rightarrow x = \frac{6-3i-2i+i^{2}}{2^{2}-i^{2}} \text{ or } \frac{4-2i}{2^{2}-i^{2}}$$
  

$$\Rightarrow x = \frac{6-5i+(-1)}{4-(-1)} \text{ or } \frac{4-2i}{4-(-1)} [\because i^{2} = -1]$$
  

$$\Rightarrow x = \frac{5-5i}{4+1} \text{ or } \frac{4-2i}{5}$$
  

$$\therefore x = 1-i \text{ or } \frac{4}{5} - \frac{2}{5}i$$

Thus, the roots of the given equation are 1 – i and  $\frac{4}{5} - \frac{2}{5}i$ .

#### 2 D. Question

Solve the following quadratic equations:

$$x^{2} - (2 + i)x - (1 - 7i) = 0$$

#### Answer

$$x^{2} - (2 + i)x - (1 - 7i) = 0$$
  
Given  $x^{2} - (2 + i)x - (1 - 7i) = 0$ 

Recall that the roots of quadratic equation  $ax^2 + bx + c = 0$ , where  $a \neq 0$ , are given by

$$\mathbf{x} = \frac{-\mathbf{b} \pm \sqrt{\mathbf{b}^2 - 4\mathbf{a}\mathbf{c}}}{2\mathbf{a}}$$

Here, a = 1, b = -(2 + i) and c = -(1 - 7i)

$$\Rightarrow x = \frac{-(-(2+i)) \pm \sqrt{(-(2+i))^2 - 4(1)(-(1-7i))}}{2(1)}$$
$$\Rightarrow x = \frac{(2+i) \pm \sqrt{(2+i)^2 + 4(1-7i)}}{2}$$
$$\Rightarrow x = \frac{(2+i) \pm \sqrt{4+4i+i^2 + 4-28i}}{2}$$



$$\Rightarrow x = \frac{(2+i) \pm \sqrt{8 - 24i + i^2}}{2}$$

By substituting  $i^2 = -1$  in the above equation, we get

$$\mathbf{x} = \frac{(2+i) \pm \sqrt{8 - 24i + (-1)}}{2}$$
  

$$\Rightarrow \mathbf{x} = \frac{(2+i) \pm \sqrt{7 - 24i}}{2}$$
  
We can write 7 - 24i = 16 - 9 - 24i  

$$\Rightarrow 7 - 24i = 16 + 9(-1) - 24i$$
  

$$\Rightarrow 7 - 24i = 16 + 9i^2 - 24i [\because i^2 = -1]$$
  

$$\Rightarrow 7 - 24i = 4^2 + (3i)^2 - 2(4)(3i)$$
  

$$\Rightarrow 7 - 24i = (4 - 3i)^2 [\because (a - b)^2 = a^2 - b^2 + 2ab]$$

By using the result 7 -  $24i = (4 - 3i)^2$ , we get

$$x = \frac{(2+i) \pm \sqrt{(4-3i)^2}}{2}$$
  
⇒  $x = \frac{(2+i) \pm (4-3i)}{2}$   
⇒  $x = \frac{(2+i) + (4-3i)}{2}$  or  $\frac{(2+i) - (4-3i)}{2}$   
⇒  $x = \frac{2+i+4-3i}{2}$  or  $\frac{2+i-4+3i}{2}$   
⇒  $x = \frac{6-2i}{2}$  or  $\frac{-2+4i}{2}$   
⇒  $x = \frac{2(3-i)}{2}$  or  $\frac{2(-1+2i)}{2}$   
∴  $x = 3-i$  or  $-1+2i$ 

Thus, the roots of the given equation are 3 - i and -1 + 2i.

#### 2 E. Question

Solve the following quadratic equations:

$$ix^2 - 4x - 4i = 0$$

### Answer

 $ix^{2} - 4x - 4i = 0$ Given  $ix^{2} - 4x - 4i = 0$   $\Rightarrow ix^{2} + 4x(-1) - 4i = 0$ We have  $i^{2} = -1$ By substituting  $-1 = i^{2}$  in the above equation, we get  $ix^{2} + 4xi^{2} - 4i = 0$   $\Rightarrow i(x^{2} + 4ix - 4) = 0$  $\Rightarrow x^{2} + 4ix - 4 = 0$ 



 $\Rightarrow x^{2} + 4ix + 4(-1) = 0$   $\Rightarrow x^{2} + 4ix + 4i^{2} = 0 [\because i^{2} = -1]$   $\Rightarrow x^{2} + 2ix + 2ix + 4i^{2} = 0$   $\Rightarrow x(x + 2i) + 2i(x + 2i) = 0$   $\Rightarrow (x + 2i)(x + 2i) = 0$   $\Rightarrow (x + 2i)^{2} = 0$   $\Rightarrow x + 2i = 0$  $\therefore x = -2i \text{ (double root)}$ 

Thus, the roots of the given equation are -2i and -2i.

## 2 F. Question

Solve the following quadratic equations:

 $x^2 + 4ix - 4 = 0$ 

#### Answer

 $x^{2} + 4ix - 4 = 0$ Given  $x^{2} + 4ix - 4 = 0$   $\Rightarrow x^{2} + 4ix + 4(-1) = 0$ We have  $i^{2} = -1$ By substituting  $-1 = i^{2}$  in the above equation, we get  $\Rightarrow x^{2} + 4ix + 4i^{2} = 0$   $\Rightarrow x^{2} + 2ix + 2ix + 4i^{2} = 0$   $\Rightarrow x(x + 2i) + 2i(x + 2i) = 0$   $\Rightarrow (x + 2i)(x + 2i) = 0$   $\Rightarrow (x + 2i)^{2} = 0$   $\Rightarrow x + 2i = 0$  $\therefore x = -2i$  (double root)

Thus, the roots of the given equation are -2i and -2i.

#### 2 G. Question

Solve the following quadratic equations:

$$2x^2 + \sqrt{15}ix - i = 0$$

#### Answer

 $2x^2 + \sqrt{15}ix - i = 0$ 

Given  $2x^2 + \sqrt{15}ix - i = 0$ 

Recall that the roots of quadratic equation  $ax^2 + bx + c = 0$ , where  $a \neq 0$ , are given by

$$\mathbf{x} = \frac{-\mathbf{b} \pm \sqrt{\mathbf{b}^2 - 4\mathbf{ac}}}{2\mathbf{a}}$$
  
Here, a = 2, b =  $\sqrt{15}\mathbf{i}$  and c = -i





$$\Rightarrow x = \frac{-(\sqrt{15}i) \pm \sqrt{(\sqrt{15}i)^2 - 4(2)(-i)}}{2(2)}$$
$$\Rightarrow x = \frac{-\sqrt{15}i \pm \sqrt{15i^2 + 8i}}{4}$$

By substituting  $i^2 = -1$  in the above equation, we get

$$x = \frac{-\sqrt{15}i \pm \sqrt{15(-1) + 8i}}{4}$$
$$\Rightarrow x = \frac{-\sqrt{15}i \pm \sqrt{8i - 15}}{4}$$
$$\Rightarrow x = \frac{-\sqrt{15}i \pm \sqrt{(-1)(15 - 8i)}}{4}$$

By substituting  $-1 = i^2$  in the above equation, we get

$$x = \frac{-\sqrt{15}i \pm \sqrt{i^2(15 - 8i)}}{4}$$
  

$$\Rightarrow x = \frac{-\sqrt{15}i \pm i\sqrt{15 - 8i}}{4}$$
  
We can write 15 - 8i = 16 - 1 - 8i  

$$\Rightarrow 15 - 8i = 16 + (-1) - 8i$$
  

$$\Rightarrow 15 - 8i = 16 + i^2 - 8i [\because i^2 = -1]$$
  

$$\Rightarrow 15 - 8i = 4^2 + (i)^2 - 2(4)(i)$$

$$\Rightarrow 15 - 8i = (4 - i)^2 [\because (a - b)^2 = a^2 - b^2 + 2ab]$$

By using the result  $15 - 8i = (4 - i)^2$ , we get

$$x = \frac{-\sqrt{15i} \pm i\sqrt{(4-i)^2}}{4}$$
  

$$\Rightarrow x = \frac{-\sqrt{15i} \pm i(4-i)}{4}$$
  

$$\Rightarrow x = \frac{-\sqrt{15i} + i(4-i)}{4} \text{ or } \frac{-\sqrt{15i} - i(4-i)}{4}$$
  

$$\Rightarrow x = \frac{-\sqrt{15i} + 4i - i^2}{4} \text{ or } \frac{-\sqrt{15i} - 4i + i^2}{4}$$
  

$$\Rightarrow x = \frac{-\sqrt{15i} + 4i - (-1)}{4} \text{ or } \frac{-\sqrt{15i} - 4i - (-1)}{4} [\because i^2 = -1]$$
  

$$\Rightarrow x = \frac{-\sqrt{15i} + 4i + 1}{4} \text{ or } \frac{-\sqrt{15i} - 4i - 1}{4}$$
  

$$\Rightarrow x = \frac{-\sqrt{15i} + 4i + 1}{4} \text{ or } \frac{-\sqrt{15i} - 4i - 1}{4}$$
  

$$\Rightarrow x = \frac{1 + (4 - \sqrt{15})i}{4} \text{ or } \frac{-1 - (4 + \sqrt{15})i}{4}$$
  

$$\therefore x = \frac{1}{4} + \left(\frac{4 - \sqrt{15}}{4}\right)i \text{ or } -\frac{1}{4} - \left(\frac{4 + \sqrt{15}}{4}\right)i$$

Thus, the roots of the given equation are  $\frac{1}{4} + \left(\frac{4-\sqrt{15}}{4}\right)i$  and  $-\frac{1}{4} - \left(\frac{4+\sqrt{15}}{4}\right)i$ .

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## 2 H. Question

Solve the following quadratic equations:

$$x^2 - x + (1 + i) = 0$$

#### Answer

 $x^{2} - x + (1 + i) = 0$ Given  $x^{2} - x + (1 + i) = 0$ 

Recall that the roots of quadratic equation  $ax^2 + bx + c = 0$ , where  $a \neq 0$ , are given by

$$\mathbf{x} = \frac{-\mathbf{b} \pm \sqrt{\mathbf{b}^2 - 4\mathbf{a}\mathbf{c}}}{2\mathbf{a}}$$

Here, a = 1, b = -1 and c = (1 + i)

$$\Rightarrow x = \frac{-(-1) \pm \sqrt{(-1)^2 - 4(1)(1+i)}}{2(1)}$$
$$\Rightarrow x = \frac{1 \pm \sqrt{1 - 4(1+i)}}{2}$$
$$\Rightarrow x = \frac{1 \pm \sqrt{1 - 4 - 4i}}{2}$$
$$\Rightarrow x = \frac{1 \pm \sqrt{-3 - 4i}}{2}$$
$$\Rightarrow x = \frac{1 \pm \sqrt{(-3 - 4i)}}{2}$$

By substituting  $-1 = i^2$  in the above equation, we get

$$x = \frac{1 \pm \sqrt{i^2(3+4i)}}{2}$$
  

$$\Rightarrow x = \frac{1 \pm i\sqrt{3+4i}}{2}$$
  
We can write 3 + 4i = 4 - 1 + 4i  

$$\Rightarrow 3 + 4i = 4 + i^2 + 4i [\because i^2 = -1]$$
  

$$\Rightarrow 3 + 4i = 2^2 + i^2 + 2(2)(i)$$
  

$$\Rightarrow 3 + 4i = (2 + i)^2 [\because (a + b)^2 = a^2 + b^2 + 2ab]$$

By using the result  $3 + 4i = (2 + i)^2$ , we get

$$x = \frac{1 \pm i\sqrt{(2-i)^2}}{2}$$
  

$$\Rightarrow x = \frac{1 \pm i(2+i)}{2}$$
  

$$\Rightarrow x = \frac{1 + i(2+i)}{2} \text{ or } \frac{1 - i(2+i)}{2}$$
  

$$\Rightarrow x = \frac{1 + 2i + i^2}{2} \text{ or } \frac{1 - 2i - i^2}{2}$$
  

$$\Rightarrow x = \frac{1 + 2i + (-1)}{2} \text{ or } \frac{1 - 2i - (-1)}{2} [\because i^2 = -1]$$



$$\Rightarrow x = \frac{1+2i-1}{2} \text{ or } \frac{1-2i+1}{2}$$
$$\Rightarrow x = \frac{2i}{2} \text{ or } \frac{2-2i}{2}$$
$$\Rightarrow x = i \text{ or } \frac{2(1-i)}{2}$$
$$\therefore x = i \text{ or } 1-i$$

Thus, the roots of the given equation are i and 1 - i.

### 2 I. Question

Solve the following quadratic equations:

 $ix^2 - x + 12i = 0$ Answer  $ix^2 - x + 12i = 0$ Given  $ix^2 - x + 12i = 0$  $\Rightarrow ix^{2} + x(-1) + 12i = 0$ We have  $i^2 = -1$ By substituting  $-1 = i^2$  in the above equation, we get  $ix^2 + xi^2 + 12i = 0$  $\Rightarrow i(x^2 + ix + 12) = 0$  $\Rightarrow x^2 + ix + 12 = 0$  $\Rightarrow x^{2} + ix - 12(-1) = 0$  $\Rightarrow x^{2} + ix - 12i^{2} = 0$  [::  $i^{2} = -1$ ]  $\Rightarrow x^2 - 3ix + 4ix - 12i^2 = 0$  $\Rightarrow x(x - 3i) + 4i(x - 3i) = 0$  $\Rightarrow$  (x - 3i)(x + 4i) = 0  $\Rightarrow$  x - 3i = 0 or x + 4i = 0  $\therefore x = 3i \text{ or } -4i$ 

Thus, the roots of the given equation are 3i and -4i.

## 2 J. Question

Solve the following quadratic equations:

$$x^2 - \left(3\sqrt{2} - 2i\right)x - \sqrt{2}i = 0$$

#### Answer

$$\begin{aligned} x^2 - (3\sqrt{2} - 2i)x - \sqrt{2}i &= 0\\ \text{Given } x^2 - (3\sqrt{2} - 2i)x - \sqrt{2}i &= 0 = 0 \end{aligned}$$

Recall that the roots of quadratic equation  $ax^2 + bx + c = 0$ , where  $a \neq 0$ , are given by

$$\mathbf{x} = \frac{-\mathbf{b} \pm \sqrt{\mathbf{b}^2 - 4\mathbf{a}\mathbf{c}}}{2\mathbf{a}}$$





Here, 
$$a = 1, b = -(3\sqrt{2} - 2i)$$
 and  $c = -\sqrt{2}i$   

$$\Rightarrow x = \frac{-(-(3\sqrt{2} - 2i)) \pm \sqrt{(-(3\sqrt{2} - 2i))^2 - 4(1)(-\sqrt{2}i)}}{2(1)}$$

$$\Rightarrow x = \frac{(3\sqrt{2} - 2i) \pm \sqrt{(3\sqrt{2} - 2i)^2 + 4\sqrt{2}i}}{2}$$

$$\Rightarrow x = \frac{(3\sqrt{2} - 2i) \pm \sqrt{18 - 12\sqrt{2}i + 4i^2 + 4\sqrt{2}i}}{2}$$

$$\Rightarrow x = \frac{(3\sqrt{2} - 2i) \pm \sqrt{18 - 8\sqrt{2}i + 4i^2}}{2}$$

By substituting  $i^2$  = -1 in the above equation, we get

$$x = \frac{(3\sqrt{2} - 2i) \pm \sqrt{18 - 8\sqrt{2}i + 4(-1)}}{2}$$

$$\Rightarrow x = \frac{(3\sqrt{2} - 2i) \pm \sqrt{18 - 8\sqrt{2}i - 4}}{2}$$

$$\Rightarrow x = \frac{(3\sqrt{2} - 2i) \pm \sqrt{14 - 8\sqrt{2}i}}{2}$$
We can write  $14 - 8\sqrt{2}i = 16 - 2 - 8\sqrt{2}i$ 

$$\Rightarrow 14 - 8\sqrt{2}i = 16 + 2(-1) - 8\sqrt{2}i$$

$$\Rightarrow 14 - 8\sqrt{2}i = 16 + 2i^2 - 8\sqrt{2}i [\because i^2 = -1]$$

$$\Rightarrow 14 - 8\sqrt{2}i = 4^2 + (\sqrt{2}i)^2 - 2(4)(\sqrt{2}i)$$

$$\Rightarrow 14 - 8\sqrt{2}i = (4 - \sqrt{2}i)^2 [\because (a - b)^2 = a^2 - 2ab + b^2]$$
By using the result  $14 - 8\sqrt{2}i = (4 - \sqrt{2}i)^2$ , we get

$$x = \frac{(3\sqrt{2} - 2i) \pm \sqrt{(4 - \sqrt{2}i)^2}}{2}$$
  

$$\Rightarrow x = \frac{(3\sqrt{2} - 2i) \pm (4 - \sqrt{2}i)}{2}$$
  

$$\Rightarrow x = \frac{(3\sqrt{2} - 2i) + (4 - \sqrt{2}i)}{2} \text{ or } \frac{(3\sqrt{2} - 2i) - (4 - \sqrt{2}i)}{2}$$
  

$$\Rightarrow x = \frac{3\sqrt{2} - 2i + 4 - \sqrt{2}i}{2} \text{ or } \frac{3\sqrt{2} - 2i - 4 + \sqrt{2}i}{2}$$
  

$$\Rightarrow x = \frac{3\sqrt{2} + 4 - (2 + \sqrt{2}i)}{2} \text{ or } \frac{3\sqrt{2} - 4 - (2 - \sqrt{2})i}{2} [\because i^2 = -1]$$
  

$$\Rightarrow x = \frac{3\sqrt{2} + 4}{2} - \left(\frac{2 + \sqrt{2}}{2}\right)i \text{ or } \frac{3\sqrt{2} - 4}{2} - \left(\frac{2 - \sqrt{2}}{2}\right)i$$
  
Thus, the roots of the given equation are  $\frac{3\sqrt{2} + 4}{2} - \left(\frac{2 + \sqrt{2}}{2}\right)i \text{ or } \frac{3\sqrt{2} - 4}{2} - \left(\frac{2 - \sqrt{2}}{2}\right)i$   
**2 K. Question**

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Solve the following quadratic equations:

$$x^2 - \left(\sqrt{2} + i\right)x + \sqrt{2}i = 0$$

#### Answer

 $xi. x^{2} - (\sqrt{2} + i)x + \sqrt{2}i = 0$ Given  $x^{2} - (\sqrt{2} + i)x + \sqrt{2}i = 0$   $\Rightarrow x^{2} - (\sqrt{2}x + ix) + \sqrt{2}i = 0$   $\Rightarrow x^{2} - \sqrt{2}x - ix + \sqrt{2}i = 0$   $\Rightarrow x(x - \sqrt{2}) - i(x - \sqrt{2}) = 0$   $\Rightarrow (x - \sqrt{2})(x - i) = 0$   $\Rightarrow x - \sqrt{2} = 0 \text{ or } x - i = 0$  $\therefore x = \sqrt{2} \text{ or } i$ 

Thus, the roots of the given equation are  $\sqrt{2}$  and i.

### 2 L. Question

Solve the following quadratic equations:

 $2x^2 - (3 + 7i)x + (9i - 3) = 0$ 

#### Answer

 $2x^2 - (3 + 7i)x + (9i - 3) = 0$ 

Given  $2x^2 - (3 + 7i)x + (9i - 3) = 0$ 

Recall that the roots of quadratic equation  $ax^2 + bx + c = 0$ , where  $a \neq 0$ , are given by

$$\mathbf{x} = \frac{-\mathbf{b} \pm \sqrt{\mathbf{b}^2 - 4\mathbf{a}\mathbf{c}}}{2\mathbf{a}}$$

Here, a = 2, b = -(3 + 7i) and c = (9i - 3)

$$\Rightarrow x = \frac{-(-(3+7i)) \pm \sqrt{(-(3+7i))^2 - 4(2)(9i-3)}}{2(2)}$$

$$\Rightarrow x = \frac{(3+7i) \pm \sqrt{(3+7i)^2 - 8(9i-3)}}{4}$$

$$\Rightarrow x = \frac{(3+7i) \pm \sqrt{9+42i+49i^2-72i+24}}{4}$$

$$\Rightarrow x = \frac{(3+7i) \pm \sqrt{33-30i+49i^2}}{4}$$

By substituting  $i^2 = -1$  in the above equation, we get

$$x = \frac{(3+7i) \pm \sqrt{33 - 30i + 49(-1)}}{4}$$
$$\Rightarrow x = \frac{(3+7i) \pm \sqrt{33 - 30i - 49}}{4}$$



$$\Rightarrow x = \frac{(3+7i) \pm \sqrt{-16-30i}}{4}$$
$$\Rightarrow x = \frac{(3+7i) \pm \sqrt{(-1)(16+30i)}}{4}$$

By substituting  $-1 = i^2$  in the above equation, we get

$$\mathbf{x} = \frac{(3+7i) \pm \sqrt{i^2(16+30i)}}{4}$$
  

$$\Rightarrow \mathbf{x} = \frac{(3+7i) \pm i\sqrt{16+30i}}{4}$$
  
We can write 16 + 30i = 25 - 9 + 30i  

$$\Rightarrow 16 + 30i = 25 + 9(-1) + 30i$$
  

$$\Rightarrow 16 + 30i = 25 + 9i^2 + 30i [\because i^2 = -1]$$
  

$$\Rightarrow 16 + 30i = 5^2 + (3i)^2 + 2(5)(3i)$$
  

$$\Rightarrow 16 + 30i = (5 + 3i)^2 [\because (a + b)^2 = a^2 + b^2 + 2ab]$$

By using the result  $16 + 30i = (5 + 3i)^2$ , we get

$$x = \frac{(3+7i) \pm i\sqrt{(5+3i)^2}}{4}$$
  

$$\Rightarrow x = \frac{(3+7i) \pm i(5+3i)}{4} \text{ or } \frac{(3+7i) - i(5+3i)}{4}$$
  

$$\Rightarrow x = \frac{(3+7i) + i(5+3i)}{4} \text{ or } \frac{(3+7i) - i(5+3i)}{4}$$
  

$$\Rightarrow x = \frac{3+7i + 5i + 3i^2}{4} \text{ or } \frac{3+7i - 5i - 3i^2}{4}$$
  

$$\Rightarrow x = \frac{3+12i + 3i^2}{4} \text{ or } \frac{3+2i - 3i^2}{4}$$
  

$$\Rightarrow x = \frac{3+12i + 3(-1)}{4} \text{ or } \frac{3+2i - 3(-1)}{4} [\because i^2 = -1]$$
  

$$\Rightarrow x = \frac{3+12i - 3}{4} \text{ or } \frac{3+2i + 3}{4}$$
  

$$\Rightarrow x = \frac{3+12i - 3}{4} \text{ or } \frac{3+2i + 3}{4}$$
  

$$\Rightarrow x = \frac{12}{4} \text{ i or } \frac{6+2i}{4}$$
  

$$\Rightarrow x = 3i \text{ or } \frac{6}{4} + \frac{2}{4}i$$
  

$$\therefore x = 3i \text{ or } \frac{3}{2} + \frac{1}{2}i$$

Thus, the roots of the given equation are 3i and  $\frac{3}{2} + \frac{1}{2}i$ .

#### **Very Short Answer**

## 1. Question

Write the number of real roots of the equation  $(x-1)^2 + (x-2)^2 + (x-3)^2 = 0$ .

## Answer

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given  $(x-1)^2 + (x-2)^2 + (x-3)^2 = 0$   $x^2 + 1 - 2x + X^2 + 4 - 4x + X^2 + 9 - 6x = 0$  $3X^2 - 12x + 14 = 0$ 

Comparing it with  $aX^2 + bx + c = 0$  and substituting them in  $b^2 - 4ac$ , we get

 $= (-12)^2 - 4(3)(14)$ 

= 144 - 168

= - 24 < 0.

Hence the given equation do not have real roots. It has imaginary roots.

### 2. Question

If a and b are roots of the equation  $x^2 - px + q = 0$ , then write the value of  $\frac{1}{a} + \frac{1}{b}$ .

### Answer

given  $x^2 - px + q = 0$ 

We know sum of the roots = p

Product of the roots = q

As given that a and b are roots then,

a + b = p a b = qgiven  $\frac{1}{a} + \frac{1}{b}$   $= \frac{a + b}{ab}$  $= \frac{p}{q}.$ 

## 3. Question

If roots  $\alpha$ ,  $\beta$  of equation  $x^2 - px + 16 = 0$  satisfy the relation  $\alpha^2 + \beta^2 = 9$ , then write the value of p.

## Answer

given  $\alpha^2 + \beta^2 = 9$   $(\alpha + \beta)^2 - 2 \alpha \beta = 9$ Given  $x^2$ - px + 16 = 0 and  $\alpha$ ,  $\beta$  are roots of the equation then Sum of roots  $\alpha + \beta = p$ Product of roots  $\alpha \beta = 16$ Substituting these in  $(\alpha + \beta)^2 - 2 \alpha \beta = 9$  we get,  $p^2 - 2(16) = 9$   $p^2 = 41$   $P = \pm \sqrt{41}$ 4. Question





If  $2 + \sqrt{3}$  is a root of the equation  $x^2 + px + q = 0$ , then write the values of p and q.

#### Answer

we know irrational roots always exists in pair hence if  $2 + \sqrt{3}$  is one root then  $2 - \sqrt{3}$  is another root.

```
Given x^2 + px + q = 0

Sum of roots = -p

2+\sqrt{3}+2-\sqrt{3} = -p

P = -4

Product of roots = q

(2+\sqrt{3})(2-\sqrt{3})=q

4-3=q

q = 1.
```

#### 5. Question

If the difference between the roots of the equation  $x^2 + ax + 8 = 0$  is 2 write the values of a.

#### Answer

given  $x^2 + ax + 8 = 0$  and  $\alpha - \beta = 2$ Also from given equation  $\alpha \beta = 8$ As  $\alpha - \beta = 2$ Then  $\alpha - \frac{\alpha}{\alpha} = 2$  $\alpha^2 - 2 \alpha - 8 = 0$  $(\alpha - 4) (\alpha + 2) = 0$  $\alpha = 4$  and  $\alpha = -2$ if  $\alpha = 4$  then substituting it in  $\alpha - \beta = 2$  we get ,  $\beta = 2$ from the given equation, sum of roots = -a  $\alpha + \beta = -a$ - a = 4+2 a = -6 if  $\alpha = -2$  then substituting it in  $\alpha - \beta = 2$  we get ,  $\beta = -4$ then sum of roots  $\alpha + \beta = -a$ a = 6 therefore  $a = \pm 6$ . 6. Question Write the roots of the equation  $(a-b)x^2 + (b-c)x + (c-a) = 0$ Answer





roots of a quadratic equation is  $_{X}=\frac{-b\pm\sqrt{b^{2}-4ac}}{2a}$ 

From the given equation we get,

$$\begin{aligned} x &= \frac{-(b-c) \pm \sqrt{(b-c)^2 - 4(a-b)(c-a)}}{2(a-b)} \\ x &= \frac{-(b-c) \pm \sqrt{b^2 + c^2 - 2bc - 4ac + 4a^2 + 4bc - 4ab}}{2(a-b)} \\ x &= \frac{-(b-c) \pm \sqrt{(-2a+b+c)^2}}{2(a-b)} \\ &= \frac{-b+c+(-2a+b+c)}{2(a-b)} \text{ and } \frac{-b+c-(-2a+b+c)}{2(a-b)} \\ &= \frac{2(c-a)}{2(a-b)} \text{ and } \frac{2(a-b)}{2(a-b)} \\ &= \frac{2(c-a)}{2(a-b)} \text{ and } \frac{2(a-b)}{2(a-b)} \\ &= \frac{(c-a)}{(a-b)} \text{ and } 1 \\ \text{Therefore } x &= 1, \frac{(c-a)}{(a-b)}. \end{aligned}$$

## 7. Question

If a and b are roots of the equation  $x^2 - x + 1 = 0$ , then write the value of  $a^2 + b^2$ .

#### Answer

from the given equation sum of roots a + b = 1

Product of roots ab = 1

Now  $a^2 + b^2 = (a + b)^2 - 2 a b$ 

= - 1.

#### 8. Question

Write the number of quadratic equations, with real roots, which do not change by squaring their roots.

#### Answer

from the given condition roots remain unchanged only when they are equal to 1 and 0.

Hence the roots may be (0,1) or (1,0) and (1,1) and (0,0).

Hence 3 equations can be formed by substituting these points in (x-a)(x-b) = 0

Where a, b are roots or points.

#### 9. Question

If  $\alpha$ ,  $\beta$  are roots of the equation  $x^2 + lx + m = 0$ , write an equation whose roots are  $-\frac{1}{\alpha}$  and  $-\frac{1}{\beta}$ .

#### Answer

from the given equation sum of the roots  $\alpha$  +  $\beta$  = - I

Product of roots  $\alpha\beta = m$ 

Formula to form a quadratic equation is  $x^2$ - ( $\alpha + \beta$ )  $x + \alpha\beta = 0$ 





Where  $\alpha$ ,  $\beta$  are roots of equation.

Given  $\frac{-1}{\alpha}$ ,  $\frac{-1}{\beta}$  are roots, then required quadratic equation is

$$x^{2} - \left(\frac{-1}{\alpha} + \frac{-1}{\beta}\right)x + \frac{1}{\alpha\beta} = 0$$
$$x^{2} + \left(\frac{\alpha + \beta}{\alpha\beta}\right)x + \frac{1}{\alpha\beta} = 0$$
$$x^{2} + \left(\frac{-l}{m}\right)x + \frac{1}{m} = 0$$

 $mx^2 - lx + 1 = 0.$ 

## 10. Question

If  $\alpha$ ,  $\beta$  are roots of the equation  $x^2 - a(x+1) - c = 0$ , then write the value of  $(1+\alpha)(1+\beta)$ .

#### Answer

given  $x^2$ -a(x+1)-c=0  $x^2$ -ax-a-c=0  $x^2$ -ax-(a+c)=0 as  $\alpha$ ,  $\beta$  are roots of equation, we get sum of the roots  $\alpha + \beta = a$ Product of roots  $\alpha\beta = -(a + c)$ Given (1+  $\alpha$ ) (1+  $\beta$ ) = 1 + ( $\alpha$  +  $\beta$ ) + ( $\alpha$   $\beta$ ) = 1 + a - a - c = 1 - c.

## MCQ

#### 1. Question

Mark the Correct alternative in the following:

The complete set of values of k, for which the quadratic equation  ${_X}^2-k_{\!X}+k+2=0\,$  has equal rots, consists of

- A.  $2 + \sqrt{12}$
- B.  $2 \pm \sqrt{12}$
- C.  $2 \sqrt{12}$
- D.  $-2 \sqrt{12}$

# Answer

Since roots are equal then  $b^2 - 4ac = 0$ 

From the given equation we get,

 $K^2 - 4(1)(k+2) = 0$ 

 $K^2 - 4 k - 8 = 0$ 





$$k = \frac{4 \pm \sqrt{4^2 - 4(2)^2}}{2}$$
$$= \frac{4 \pm \sqrt{16 + 32}}{2}$$
$$= \frac{4 \pm \sqrt{48}}{2}$$
$$= \frac{4 \pm 2\sqrt{12}}{2}$$
$$= 2 \pm \sqrt{12}$$

#### 2. Question

Mark the Correct alternative in the following:

-8)

For the equation  $\left|x\right|^{2}+\left|x\right|-6=0$  , the sum of the real roots is

A. 1

B. 0

C. 2

D. none of these

## Answer

```
given |x|^2 + |x| - 6 = 0

When x > 0

It can be written as x^2 + x - 6 = 0

(x+3)(x-2) = 0

X = 2

When x < 0

It can be written as x^2 - x - 6 = 0

(x-3)(x+2) = 0

X = -2

Therefore x = \pm 2

Hence sum of the roots = 0.

3. Question

Mark the Correct alternative in the following:

If a, b are the roots of the equation x^2 + x + 1 = 0, then a^2 + b^2 = a^2
```

A. 1 B. 2

C. –1

D. 3

## Answer

from the given equation sum of roots a + b = -1





```
Product of roots ab = 1
Given a^2 + b^2
(a + b)^2 - 2 a b
= 1 - 2
= -1.
```

### 4. Question

Mark the Correct alternative in the following:

If  $\alpha$ ,  $\beta$  are roots of the equation  $4x^2 + 3x + 7 = 0$ , then  $1/\alpha + 1/\beta$  is equal to

A. 7/3

B. -7/3

C. 3/7

D. -3/7

### Answer

given  $4x^2 + 3x + 7 = 0$ 

We know sum of the roots  $=\frac{-3}{4}$ 

Product of the roots  $=\frac{7}{4}$ 

As given that  $\alpha$  and  $\beta$  are roots then,

 $\alpha + \beta = \frac{-3}{4}$  $\alpha \beta = \frac{7}{4}$  $given \frac{1}{\alpha} + \frac{1}{\beta}$  $= \frac{\alpha + \beta}{\alpha\beta}$  $= \frac{-\frac{3}{4}}{\frac{7}{4}}$  $= \frac{-3}{7}$ 

## 5. Question

Mark the Correct alternative in the following:

The values of x satisfying  $\log_3 \left(x^2 + 4x + 12\right) = 2$  are

A. 2, -4 B. 1, -3 C. -1, 3 D. -1, -3 **Answer** 

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given  $\log_3(x^2 + 4x + 12) = 2$ It can be written as  $\log_3(x^2 + 4x + 12) = 2\log_3 3$   $= \log_3 3^2$   $\log_3(x^2 + 4x + 12) = \log_3 9$   $x^2 + 4x + 12 = 9$   $x^2 + 4x + 3 = 0$  (x + 1) (x + 3) = 0X = -1, -3.

#### 6. Question

Mark the Correct alternative in the following:

The number of real roots of the equation  $(x^2 + 2x)^2 - (x + 1)^2 - 55 = 0$  is

- A. 2
- B. 1
- C. 4
- D. none of these

#### Answer

```
given (x^2+2x)^2 - (x+1)^2 - 55 = 0

[(x^2+2x+1) -1]^2 - (x+1)^2 - 55 = 0

(x+1)^4 - 2(x+1)^2 + 1 - (x+1)^2 - 55 = 0

(x+1)^4 - 3(x+1)^2 - 54 = 0

[t(x+1)^2 = r

r^2 - 3r - 54 = 0

r^2 - 9r + 6r - 54 = 0

r(r - 9) + 6(r - 9) = 0

r = -6, 9

but (x+1)^2 \ge 0 so, (x+1)^2 \ne -6

so, (x+1)^2 = 9

x + 1 = \pm 3

x = -1 \pm 3

x = -4, and 2.

7. Question
```

Mark the Correct alternative in the following:

If  $\alpha$ ,  $\beta$  are the roots of the equation  $ax^2 + bx + c = 0$ , then  $\frac{1}{a\alpha + b} + \frac{1}{a\beta + b} =$ 





- A. c/ab
- B. a/bc
- C. b/ac
- D. none of these

## Answer

given  $\frac{1}{a\alpha+b} + \frac{1}{a\beta+b}$  $= \frac{a\alpha+b+a\beta+b}{(a\alpha+b)(a\beta+b)}$   $= \frac{a(\alpha+\beta)+2b}{a^2(\alpha\beta)+ab(\alpha+\beta)+b^2}$   $= \frac{a(\frac{-b}{a})+2b}{a^2(\frac{c}{a})+ab(\frac{-b}{a})+b^2}$   $= \frac{b}{ac-b^2+b^2}$   $= \frac{b}{ac}$ 

# 8. Question

Mark the Correct alternative in the following:

If  $\alpha$ ,  $\beta$  are the roots of the equation  $x^2 + px + 1 = 0$ ;  $\gamma$ ,  $\delta$  the roots of the equation  $x^2 + qx + 1 = 0$ , then  $(\alpha - \gamma)(\alpha + \delta)(\beta - \gamma)(\beta + \delta) =$ A.  $q^2 - p^2$ B.  $p^2 - q^2$ C.  $p^2 + q^2$ D. none of these Answer  $\alpha^2 + p\alpha + 1 = 0, \beta^2 + p\beta + 1 = 0$  $\alpha + \beta = -p, \ \alpha\beta = 1$  $\gamma^2 + q\gamma + 1 = 0, \, \delta^2 + q\delta + 1 = 0$  $\delta - \gamma = \sqrt{q^2 - 4}, \gamma \delta = 1$  $(\alpha - \gamma)(\alpha + \delta)(\beta - \gamma)(\beta + \delta)$  $= (\alpha^2 + \alpha(\delta - \gamma) - \gamma\delta)(\beta^2 + \beta(\delta - \gamma) - \delta\gamma)$  $= \left(\alpha^2 + \alpha \sqrt{q^2 - 4} - 1\right) \left(\beta^2 + \beta \sqrt{q^2 - 4} - 1\right)$  $= \left(-2 - p\alpha + \alpha \sqrt{q^2 - 4}\right) \left(-2 - p\beta + \beta \sqrt{q^2 - 4}\right)$  $=4+2p\beta-2\beta\sqrt{q^2-4}+2p\alpha+p^2\alpha\beta-p\alpha\beta\sqrt{q^2-4}-2\alpha\sqrt{q^2-4}$  $-p\beta\alpha\sqrt{q^2-4}+\alpha^2\beta^2(q^2-4)$ 



$$= 4 + 2p(\alpha + \beta) - 2\sqrt{q^2 - 4}(\alpha + \beta) + p^2\alpha\beta - 2p\alpha\beta\sqrt{q^2 - 4} + \alpha^2\beta^2(q^2 - 4)$$
  
= 4 - 2p^2 + 2p\sqrt{q^2 - 4} + p^2 - 2p\sqrt{q^2 - 4} + (q^2 - 4)  
= 4 - 2p^2 + p^2 + q^2 - 4  
= q^2 - p^2

### 9. Question

Mark the Correct alternative in the following:

The number of real solutions of  $\left|2x-x^2-3\right|=1$  is

- A. 0
- B. 2
- C. 3
- D. 4

## Answer

given  $|2x \cdot x^2 \cdot 3| = 1$   $2x \cdot x^2 \cdot 3 = \pm 1$ When  $2x \cdot x^2 \cdot 3 = 1$   $\Rightarrow 2x \cdot x^2 \cdot 3 \cdot 1 = 0$   $\Rightarrow 2x \cdot x^2 \cdot 4 = 0$ Discriminant, D = 4 - 16 = -12 < 0Hence the roots are unreal.

When  $2x - x^2 - 3 = -1$ 

 $= x^2 - 2x - 2 = 0$ 

Discriminant, D = 4 - 8 = -4 < 0

Hence the roots are unreal.

Hence the given equation has no real roots.

## 10. Question

Mark the Correct alternative in the following:

The number of solutions of  $x^2 + \left|x - 1\right| = 1$  is

- A. 0
- B. 1
- C. 2
- D. 3
- Answer

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when x > 0  $x^{2} + x - 1 = 1$   $x^{2} + x - 2 = 0$  (x-1) (x+2) = 0 x = 1, -2when x < 0  $x^{2} - x + 1 = 1$   $x^{2} - x = 0$  x(x-1) = 0x = 0, 1

hence the given equation has 3 solutions and they are x = 0, 1, -1.

## 11. Question

Mark the Correct alternative in the following:

If x is real and 
$$k = \frac{x^2 - x + 1}{x^2 + x + 1}$$
, then  
A.  $k \in [1/3,3]$   
B.  $k \ge 3$   
C.  $k \le 1/3$   
D. none of these  
**Answer**  
 $(x^2 + x + 1)k = (x^2 - x + 1)$   
 $(k - 1)x^2 + (k + 1)x + (k - 1) = 0$   
For roots of quadratic equation real  
Case I :  $a \ne 0$  and  $D \ge 0$   
 $k - 1 \ne 0 \Rightarrow k \ne 1$   
 $\sqrt{(k + 1)^2 - 4(k - 1)(k - 1)} \ge 0$   
 $-3k^2 + 10k - 3 \ge 0$   
 $3k^2 - 10k + 3 \le 0$   
 $3(k^2 - \frac{10}{3}k + 1) \le 0$   
 $k^2 - 2(\frac{5}{3})(k) + \frac{25}{9} - \frac{25}{9} + 1 \le 0$   
 $(k - \frac{5}{3})^2 \le \frac{16}{9}$   
 $k - \frac{5}{3} \ge \frac{-4}{3}$  or  $k - \frac{5}{3} \le \frac{4}{3}$   
 $k \ge \frac{1}{3}$  or  $k \le 3$ 

Case II : a = 0

 $k - 1 = 0 \Rightarrow k = 1$ 

At k = 1,  $2x = 0 \Rightarrow x = 0$  is real

So, k = 1 is also count in answer.

Then, final answer is  $k \in [1/3, 3]$ 

# 12. Question

Mark the Correct alternative in the following:

If the roots of  $x^2 - bx + c = 0$  are two consecutive integers, then  $b^2 - 4c$  is

A. 0

B. 1

C. 2

D. None of these

# Answer

given that roots are consecutive, let they be a, a+1

From the formula for quadratic equation,

 $(x - a)(x - a - 1) = x^{2} - (a + 1)x - ax + a(a + 1) = x^{2} - (2a + 1)x + a(a + 1)thenb^{2} - 4c = (2a + 1)^{2} - 4a(a + 1) = 4a^{2} + 1 + 4a - 4a^{2} - 4a = 1.$ 

# 13. Question

Mark the Correct alternative in the following:

The value of a such that  $x^2 - 11x + a = 0$  and  $x^2 - 14x + 2a = 0$  may have a common root is

A. 0

B. 12

- C. 24
- D. 32

# Answer

subtracting both the equations we get,

$$x^{2} - 11x + a - x^{2} + 14x + 2a = 0$$
  

$$3x - a = 0$$
  

$$x = \frac{a}{3}$$
  
Substituting it in first equation we get,

$$\left(\frac{a}{3}\right)^{2} - 11\frac{a}{3} + a = 0$$
$$\frac{a^{2}}{9} - \frac{8a}{3} = 0$$
$$a^{2} - 24a = 0$$
$$a = 24.$$
**14. Question**





Mark the Correct alternative in the following:

The values of k for which is quadratic equation  $kx^2 + 1 = kx + 3x - 11x^2$  has real and equal roots are

A. -11, -3

B. 5, 7

C. 5, -7

D. None of these

### Answer

given  $kx^2 + 1 = kx + 3x - 11x^2$ 

 $x^{2}(k+11) - x(k + 3) + 1 = 0$ 

as the roots are real and equal then the discriminant is equal to zero.

 $\mathsf{D}=\mathsf{b}^2-4\mathsf{ac}=\mathsf{0}$ 

$$(k+3)^2 - 4 (k+11) (1) = 0$$
  
 $K^2 + 9 + 6k - 4k - 44 = 0$   
 $K^2 + 2k - 35 = 0$ 

(k-5)(k+7) = 0

## 15. Question

Mark the Correct alternative in the following:

If one root of the equation  $x^2 + px + 12 = 0$  is 4, while the equation  $x^2 + px + q = 0$  has equal roots, the value of q is

A. 46/4

B. 4/49

C. 4

D. none of these

## Answer

multiplying first equation and subtracting both the equations we get,

$$2x^2 + 4x + 6\lambda - 2x^2 - 3x - 5\lambda = 0$$

 $x + \lambda = 0$ 

$$\mathbf{x} = -\lambda$$

Substituting it in first equation we get,

$$(-\lambda)^2 + 2(-\lambda) + 3\lambda = 0$$

 $\lambda^2 + \lambda = 0$ 

 $\lambda = -1.$ 

# 16. Question

Mark the Correct alternative in the following:

If one root of the equation  $x^2 + px + 12 = 0$  is 4, while the equation  $x^2 + px + q = 0$  has equal roots, the

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value of q is

A. 46/4

B. 4/49

C. 4

D. none of these

## Answer

given 4 is the root of  $x^2 + px + 12 = 0$ = 16 + 4p + 12 = 0 4p = - 28 P = -7 Given  $x^2 + px + q = 0$  has equal roots, then discriminant is 0. D = b<sup>2</sup> - 4ac = 0 p<sup>2</sup> - 4q = 0 4q = 49  $q = \frac{49}{4}$ .

## 17. Question

Mark the Correct alternative in the following:

The value of p and q( $p \neq 0, q \neq 0$ ) for which p, q are the roots of the equation  $x^2 + px + q$  ab = 0 are

```
A. p = 1, q = -2

B. p = -1, q = -2

C. p = -1, q = 2

D. p = 1, q = 2

Answer

Sum of the roots = \frac{-b}{a} = -p
```

```
\Rightarrow p + q = -p \dots (1)

Product of the roots = \frac{c}{a} = q

\Rightarrow pq = q

\Rightarrow p = 1

Put value of p in eq.(1)

\Rightarrow 1 + q = -1

\Rightarrow q = -2
```

## 18. Question

Mark the Correct alternative in the following:

The set of all vales of m for which both the roots of the equation  $x^2 - (m+1)x + m + 4 = 0$  are real and negative, is

A. (−,−3] [5, ∞)





B. [-3, 5] C. (-4, -3] D. (-3, -1]

#### Answer

For roots to be real its  $D \ge 0$ 

 $\sqrt{(m + 1)^2 - 4(1)(m + 4)} \ge 0$   $(m + 1)^2 - 4(m + 4) \ge 0$   $m^2 - 2m - 15 \ge 0$   $(m - 1)^2 - 16 \ge 0$   $(m - 1)^2 \ge 16$   $m - 1 \le -4 \text{ or } m - 1 \ge 4$   $m \le -3 \text{ or } m \ge 5$ For both roots to be negative product of roots should be positive and sum of roots should be negative. Product of roots = m + 4 > 0 \Rightarrow m > -4 Sum of roots = m + 1 < 0 \Rightarrow m < -1 After taking intersection of D \ge 0, Product of roots > 0 and sum of roots < 0. We can say that the final answer is  $m \in (-4, -3]$ 

#### 19. Question

Mark the Correct alternative in the following:

The number of roots of the equation  $\frac{(x+2)(x-5)}{(x-3)(x+6)} = \frac{x-2}{x+4}$  is

A. 0

B. 1

C. 2

D. 3

#### Answer

given  $\frac{(x+2)(x-5)}{(x-3)(x+6)} = \frac{x-2}{x+4}$ (x+2) (x-5) (x+4) = (x-2) (x-3) (x+6)  $x^3+4x^2-5x^2-20x+2x^2+8x-10x-40 = x^3+6x^2-3x^2-18x-2x^2-12x+6x+36$   $x^2-22x-40 = x^2-24x+36$  4x = 76 x = 19hence the given equation has only one solution.

20. Question

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If  $\alpha$  and  $\beta$  are the roots of  $4x^2 + 3x + 7 = 0$ , then the value of  $\frac{1}{\alpha} + \frac{1}{\beta}$  is

A.  $\frac{4}{7}$ B.  $-\frac{3}{7}$ C.  $\frac{3}{7}$ D.  $-\frac{3}{4}$ 

# 4

Answer

given  $4x^2 + 3x + 7 = 0$ 

We know sum of the roots  $=\frac{-3}{4}$ 

Product of the roots  $=\frac{7}{4}$ 

As given that  $\alpha$  and  $\beta$  are roots then,

$$\alpha + \beta = \frac{-3}{4}$$
$$\alpha \beta = \frac{7}{4}$$
$$given \frac{1}{\alpha} + \frac{1}{\beta}$$
$$= \frac{\alpha + \beta}{\alpha\beta}$$
$$= \frac{-\frac{3}{4}}{\frac{7}{4}}$$
$$= \frac{-3}{7}$$

# 21. Question

Mark the Correct alternative in the following:

If  $\alpha$ ,  $\beta$  are the roots of the equation  $x^2 + px + q = 0$ , then  $-\frac{1}{\alpha}, -\frac{1}{\beta}$  are the roots of the equation

A. 
$$x^{2} - px + q = 0$$
  
B.  $x^{2} + px + q = 0$   
C.  $qx^{2} + px + 1 = 0$   
D.  $qx^{2} - px + 1 = 0$ 

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#### Answer

from the given equation sum of the roots  $\alpha$  +  $\beta$  = - p

Product of roots  $\alpha\beta = q$ 

Formula to form a quadratic equation is  $x^2$ - ( $\alpha + \beta$ ) x+  $\alpha\beta = 0$ 

- Where  $\alpha,\,\beta$  are roots of equation.
- Given  $\frac{-1}{\alpha}, \frac{-1}{\beta}$  are roots, then required quadratic equation is

$$x^{2} - \left(\frac{-1}{\alpha} + \frac{-1}{\beta}\right)x + \frac{1}{\alpha\beta} = 0$$
$$x^{2} + \left(\frac{\alpha + \beta}{\alpha\beta}\right)x + \frac{1}{\alpha\beta} = 0$$
$$x^{2} + \left(\frac{-p}{q}\right)x + \frac{1}{q} = 0$$

 $qx^2 - px + 1 = 0.$ 

# 22. Question

Mark the Correct alternative in the following:

If the difference of the roots of  $x^2-px+q=0\,$  is unity, then

A. 
$$p^{2} + 4q = 1$$
  
B.  $p^{2} - 4q = 1$   
C.  $p^{2} + 4q^{2} = (1 + 2q)^{2}$ 

D. 
$$4p^2 + q^2 = (1+2p)^2$$

# Answer

Difference of the roots =  $\frac{\sqrt{D}}{|\mathbf{a}|}$ 

$$1 = \frac{\sqrt{b^2 - 4ac}}{|a|}$$

$$1 = \frac{\sqrt{(-p)^2 - 4(1)(q)}}{|1|}$$

$$p^2 - 4q = 1$$

$$p^2 - 4q + 4q^2 - 4q^2 = 1$$

$$p^2 + 4q^2 = 1 + 2(2)(q) + (2q)^2$$

$$p^2 + 4q^2 = (1 + 2q)^2$$

# 23. Question

Mark the Correct alternative in the following:

If  $\alpha$ ,  $\beta$  are the roots of the equation  $x^2 - p(x+1) - c = 0$ , then  $(\alpha + 1)(\beta + 1) = 0$ 

А. с

B. c - 1





C. 1 – c

D. none of these

## Answer

given  $x^2 \cdot p(x+1) \cdot c = 0$   $x^2 \cdot px \cdot p \cdot c = 0$ as  $\alpha$ ,  $\beta$  are roots of equation, we get sum of the roots  $\alpha + \beta = p$ Product of roots  $\alpha\beta = -(p + c)$ Given  $(1 + \alpha) (1 + \beta)$   $= 1 + (\alpha + \beta) + (\alpha \beta)$  = 1 + p - p - c= 1 - c.

### 24. Question

Mark the Correct alternative in the following:

The least value of k which makes the roots of the equation  $x^2 + 5x + k = 0$  imaginary is

A. 4

- B. 5
- C. 6
- D. 7

## Answer

given that the equation has imaginary roots, hence the discriminant is less than 0.

= 25-4k<0

When we submit 7 in k the condition above will be satisfied and when we replace 6 the condition will be false. So the least value of k is 7.

## 25. Question

Mark the Correct alternative in the following:

The equation of the smallest degree with real coefficients having 1 + i as one of the roots is

A. 
$$x^2 + x + 1 = 0$$

B.  $x^2 - 2x + 2 = 0$ 

C.  $x^2 + 2x + 2 = 0$ 

D.  $x^2 + 2x - 2 = 0$ 

## Answer

for the complex roots it will exists in pair.

Hence the roots are 1+i and 1-i

Formula for quadratic equation is (x-a)(x-b) = 0





(x-1-i) (x-1+i) = 0 $x^{2}-x+ix-x+1-i-ix+i-i^{2}=0$  $x^{2}-2x+2 = 0.$ 



